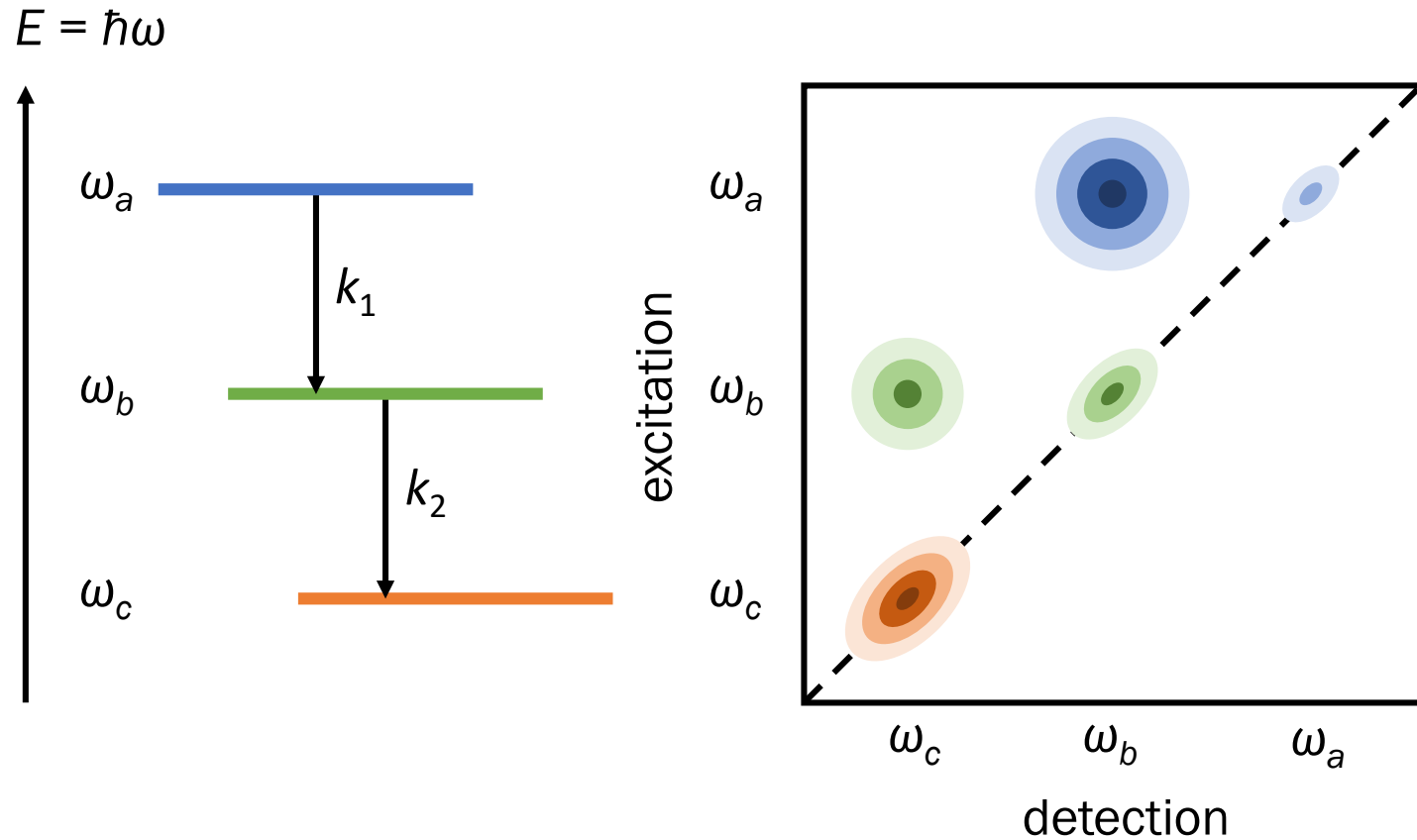


2D ELECTRONIC SPECTROSCOPY

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Biological Research Centre, Szeged

2D ELECTRONIC SPECTROSCOPY FUNDAMENTALS



Schematic 2D electronic spectrum of a coupled three-level system

2DES

- Measures the 3rd-order nonlinear optical response of the system
- Provides a time-dependent correlation map between two frequencies
- Contains all information about the system that can be gathered by any other type of 3rd-order spectroscopy:
- Electronic excited states
- Homogeneous and inhomogeneous linewidths
- Electronic couplings and coherences
- Excitation dynamics and pathways

2D ELECTRONIC SPECTROSCOPY - OUTLINE

1. Basic concepts

- Electronic transitions and spectral lines
- Homogeneous and inhomogeneous broadening
- Molecular interactions and energy transfer
- Quantum Coherence
- Molecular excitons
- Time-resolved spectroscopy
- The double resonance experiment
- Fourier transform 2DES

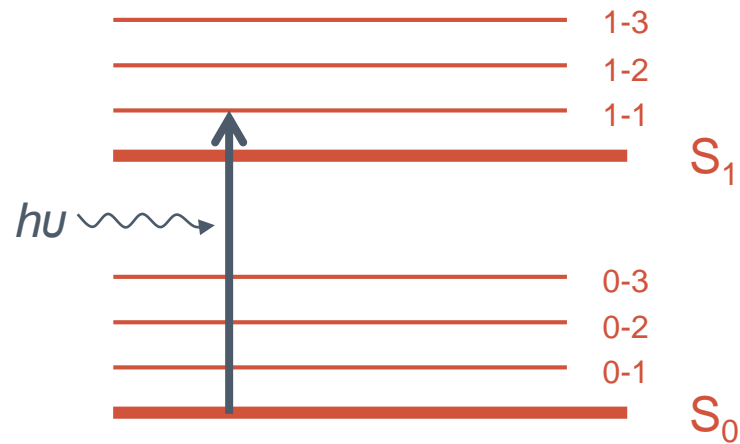
2. Technical implementations

- Boxcars vs pump-probe geometry
- Phase matching and phase cycling
- Example experimental setups

3. Application in photosynthesis

- Basics of photosynthetic light harvesting
- Energy transfer in FMO
- Energy transfer in LHCII

MOLECULAR ENERGY STATES AND TRANSITIONS



Eigenstates – solutions of the time-independent Schrödinger equation

$$E\Psi = \hat{H}\Psi$$

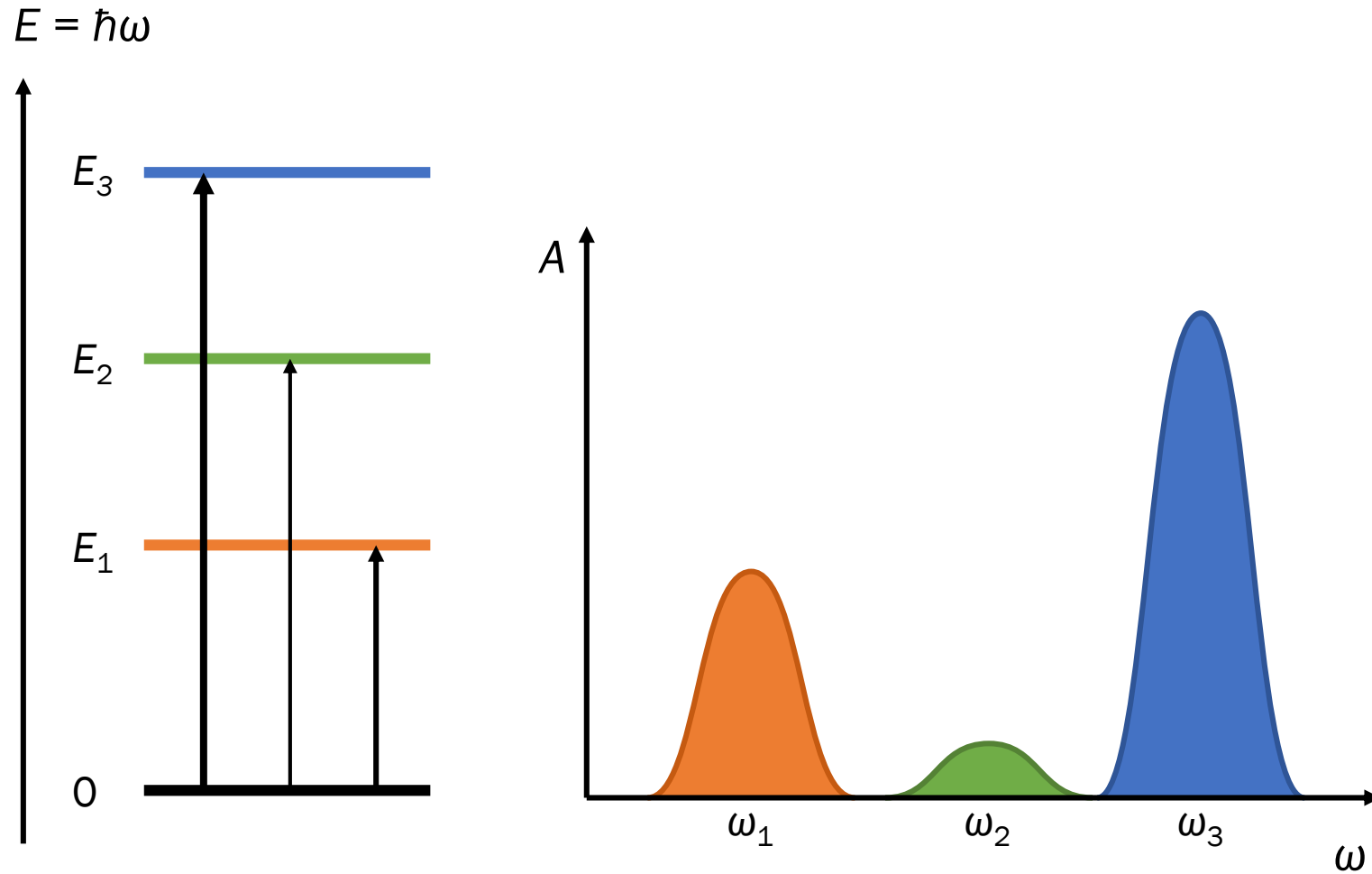
Transition dipole moment

$$\boldsymbol{\mu} = \langle \Psi_0 | \boldsymbol{\mu} | \Psi_1 \rangle = q \int \Psi_0^*(\mathbf{r}) \mathbf{r} \Psi_1(\mathbf{r}) d^3\mathbf{r}$$

Transition probability (Fermi's Golden Rule)

$$E_0^2 \cdot |\hat{\mathbf{E}} \cdot \langle \Psi_0 | \boldsymbol{\mu} | \Psi_1 \rangle|^2 = |\mathbf{E}_0|^2 \cdot |\boldsymbol{\mu}|^2 \cdot \cos^2(\hat{\mathbf{E}} \cdot \hat{\boldsymbol{\mu}})$$

ABSORPTION SPECTRA



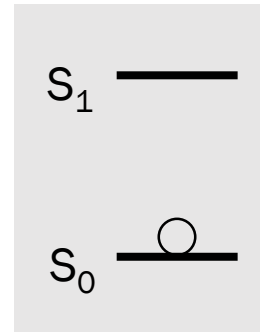
- Absorption bands correspond to energy eigenstates
- The intensity of the absorption band is proportional to the dipole strength (and chromophore concentration)

$$D = \mu^2$$

- The width of the band is controlled by homogeneous and inhomogeneous broadening effects

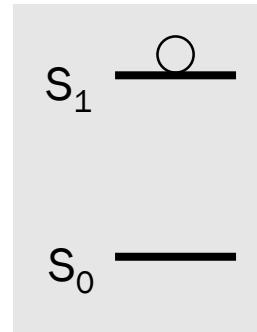
QUANTUM COHERENCE

Ground state



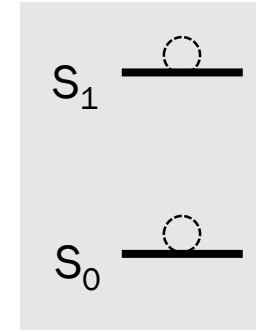
Ψ_0

Excited state



Ψ_1

Coherence state



Ψ_{01}

Density matrix

$\left \begin{array}{cc} 1 & 0 \\ 0 & 0 \end{array} \right $	$\left \begin{array}{cc} 0 & 0 \\ 0 & 1 \end{array} \right $	$\left \begin{array}{cc} 1/2 & -i/2 \\ i/2 & 1/2 \end{array} \right $
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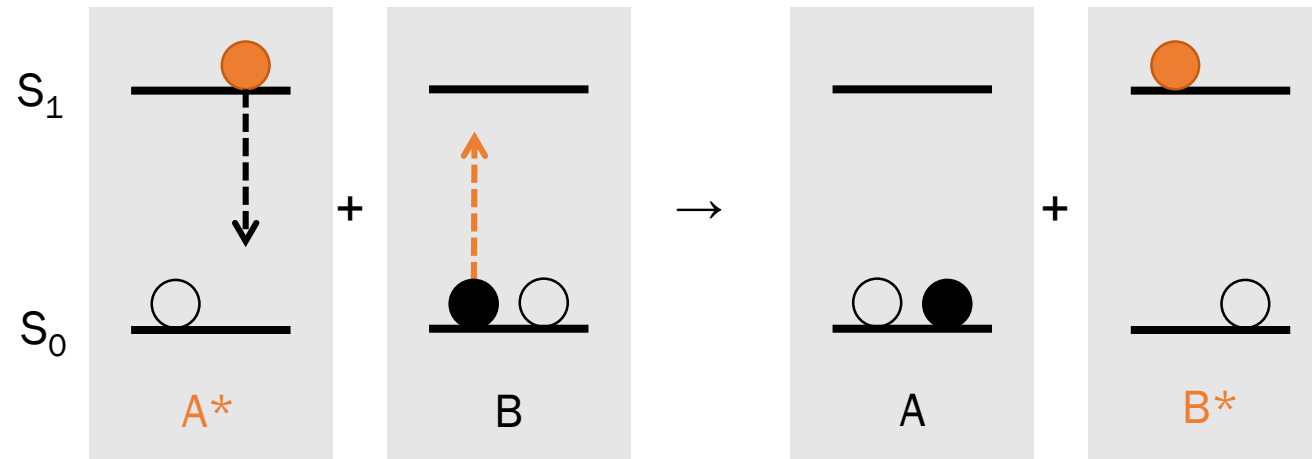
Coherent superposition of states

$$\begin{aligned} \Psi_{01} &= c_0 \Psi_0 + c_1 \Psi_1 = \\ &= c_0 \psi_0 e^{-iE_0 t/\hbar} + c_1 \psi_1 e^{-iE_1 t/\hbar} \end{aligned}$$

Oscillation frequency

$$\omega_{01} = (E_1 - E_0)/\hbar$$

EXCITATION ENERGY TRANSFER



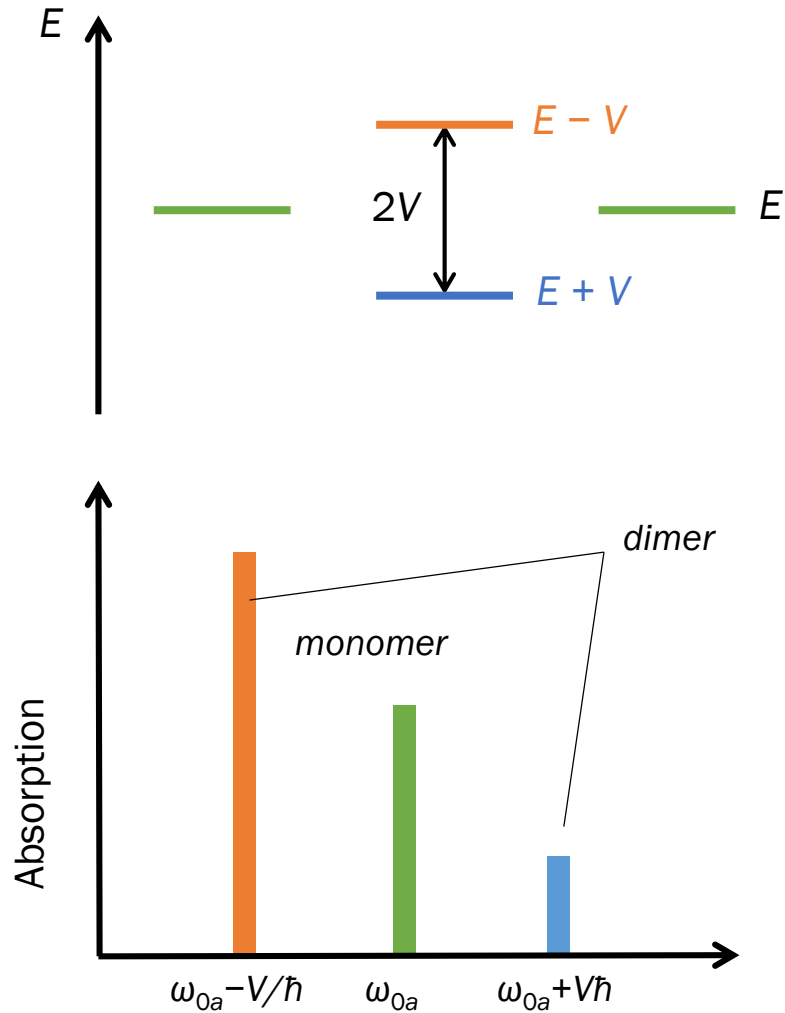
Förster resonance energy transfer

$$k_{AB} = \frac{9\kappa^2 c^4}{8\pi\tau_{A^*} n^4 R^6} \int F_A(\omega) \sigma_B(\omega) \frac{d\omega}{\omega^4}$$

Typical energy transfer times

$$10^{-14} - 10^{-9} \text{ s}$$

THE EXCITONIC DIMER



Exciton (Frenkel) Hamiltonian

$$H = H_1 + H_2 + V$$

$$V = \frac{1}{4\pi\epsilon_0 r^3} (\boldsymbol{\mu}_1 \cdot \boldsymbol{\mu}_2 - 3(\boldsymbol{\mu}_1 \cdot \hat{\mathbf{r}})(\boldsymbol{\mu}_2 \cdot \hat{\mathbf{r}}))$$

$$(H_1 + H_2 + V)\Psi_\alpha = E_\alpha \Psi_\alpha$$

$$\mathbf{H} = \begin{vmatrix} \langle \Psi_1 | H | \Psi_1 \rangle & \langle \Psi_1 | H | \Psi_2 \rangle \\ \langle \Psi_2 | H | \Psi_1 \rangle & \langle \Psi_2 | H | \Psi_2 \rangle \end{vmatrix} = \begin{vmatrix} E_1 & V \\ V & E_2 \end{vmatrix}$$

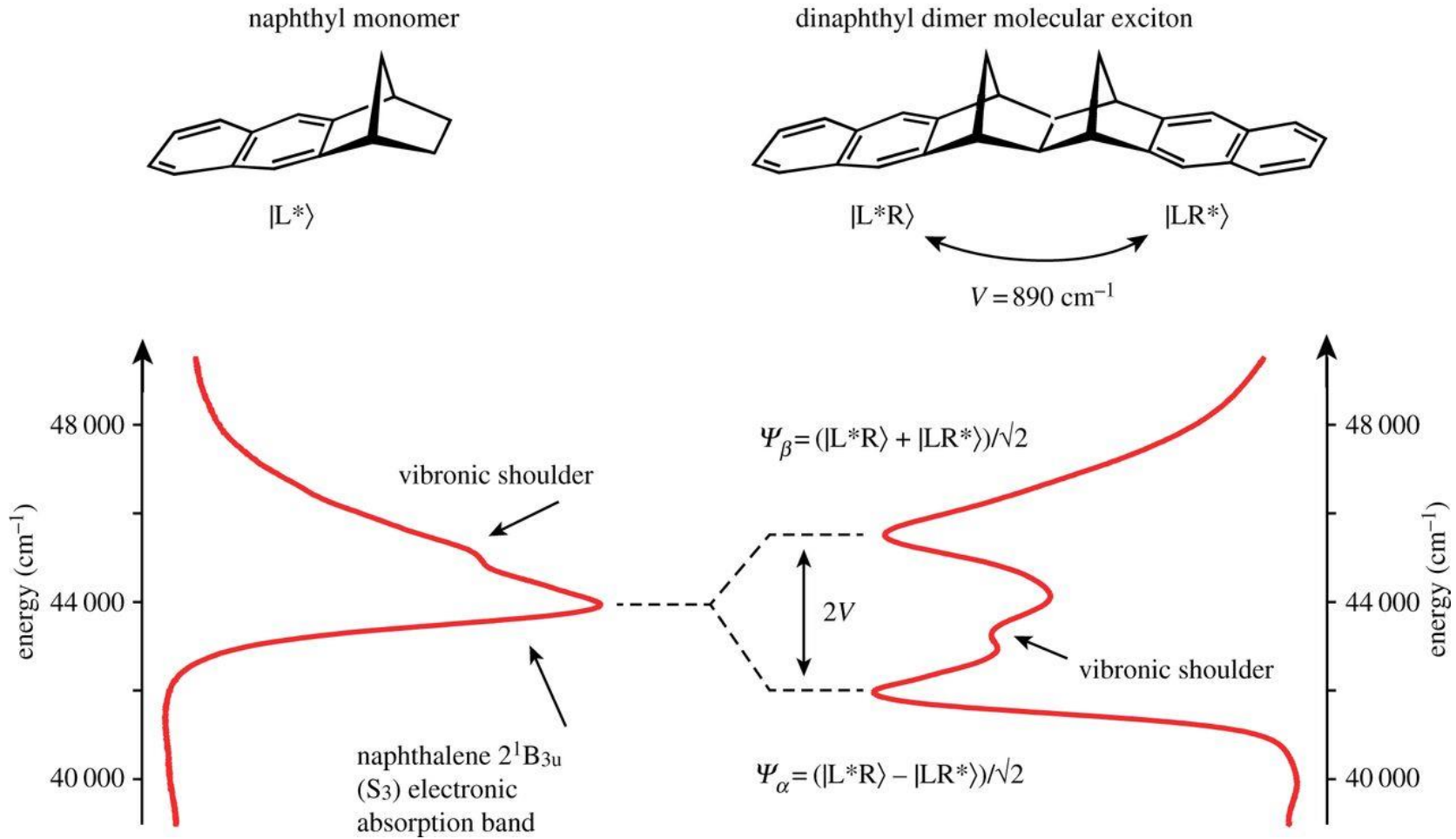
Solution - exciton states

$$E_\alpha = E \pm V$$

$$\Psi_\alpha = \frac{1}{\sqrt{2}} (\Psi_1 \pm \Psi_2)$$

$$\boldsymbol{\mu}_\alpha = \frac{1}{\sqrt{2}} (\boldsymbol{\mu}_1 \pm \boldsymbol{\mu}_2)$$

MOLECULAR EXCITONS



INCOHERENT VS. COHERENT TRANSFER

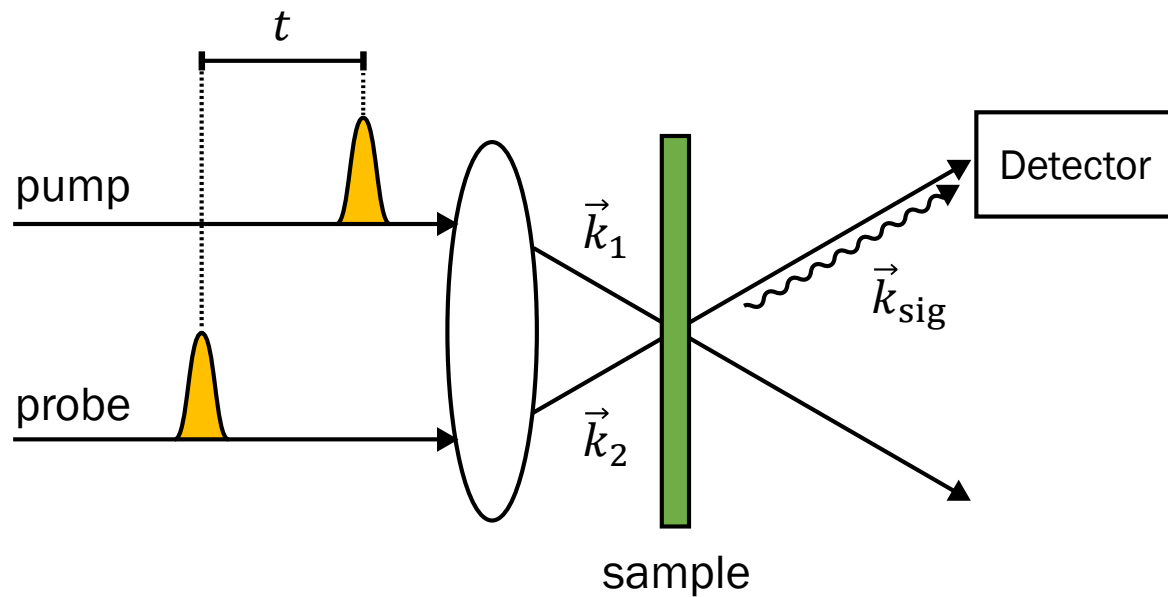
Weak coupling limit

- Weak chromophore interaction
- Localized excited states
- Vibrational relaxation is faster than energy transfer
- Incoherent hopping of excitations
- Rate of transfer depends on the the square of the dipole-dipole interaction
- Förster theory

Strong coupling limit

- Strong chromophore interaction
- Delocalized exciton states
- Energy transfer occurs before vibrational relaxation
- Wave-like excitation motions
- Rate of transfer depends on the quantum dipole-dipole interaction term
- Redfield theory

PUMP-PROBE SPECTROSCOPY



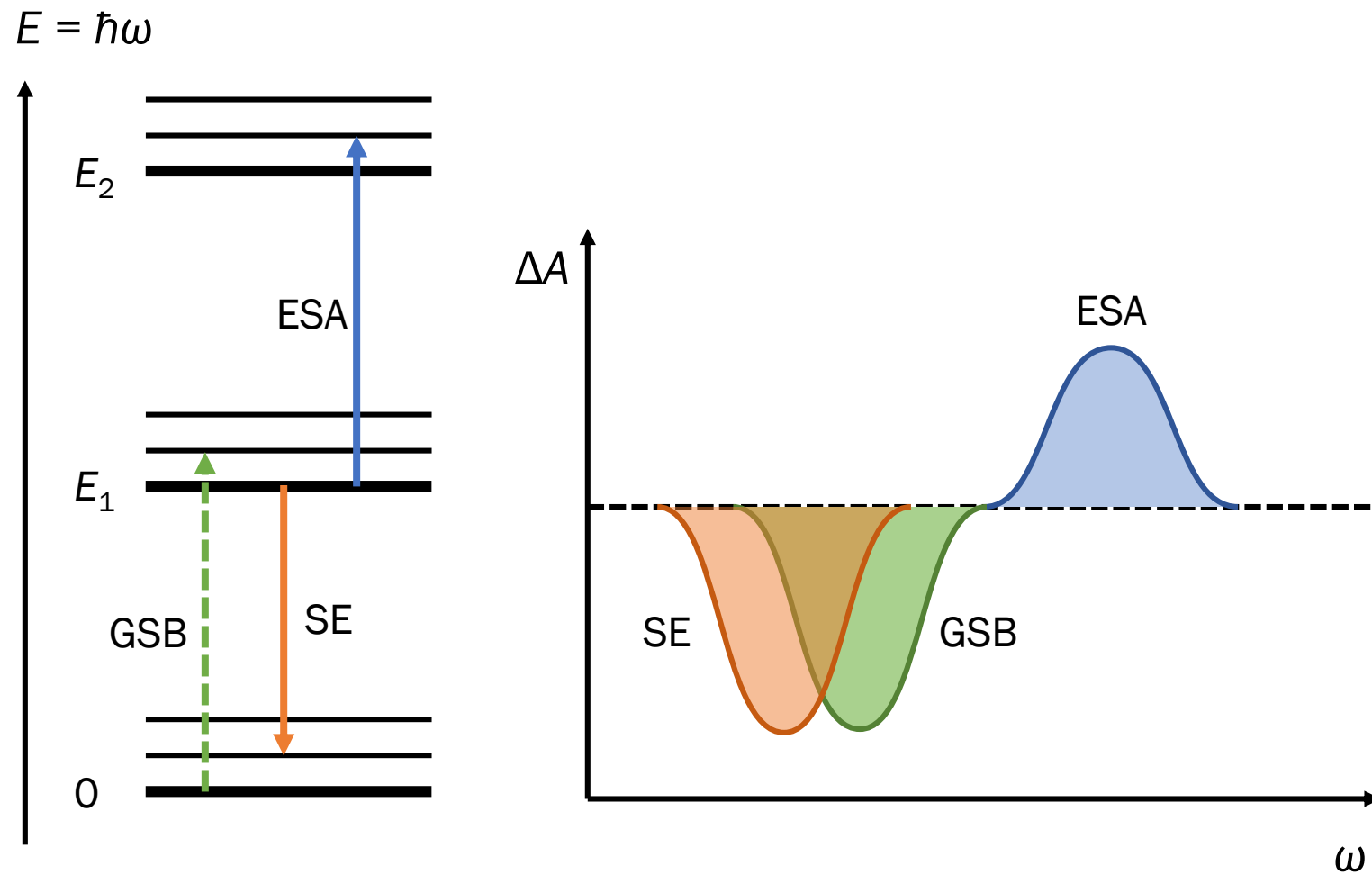
Differential absorption:

$$\Delta A(t) = A_{+pump} - A_{-pump}$$

- 'Pump' pulse creates excited states ($GS \rightarrow S_1$)
- A subsequent 'probe' pulse ($S_1 \rightarrow S_n$) measures the changes induced by the pump
- The temporal evolution is followed by scanning over the time between pump and probe
- Temporal resolution is only limited by the pulse duration
- 3rd order nonlinear spectroscopy
- Phase matching direction

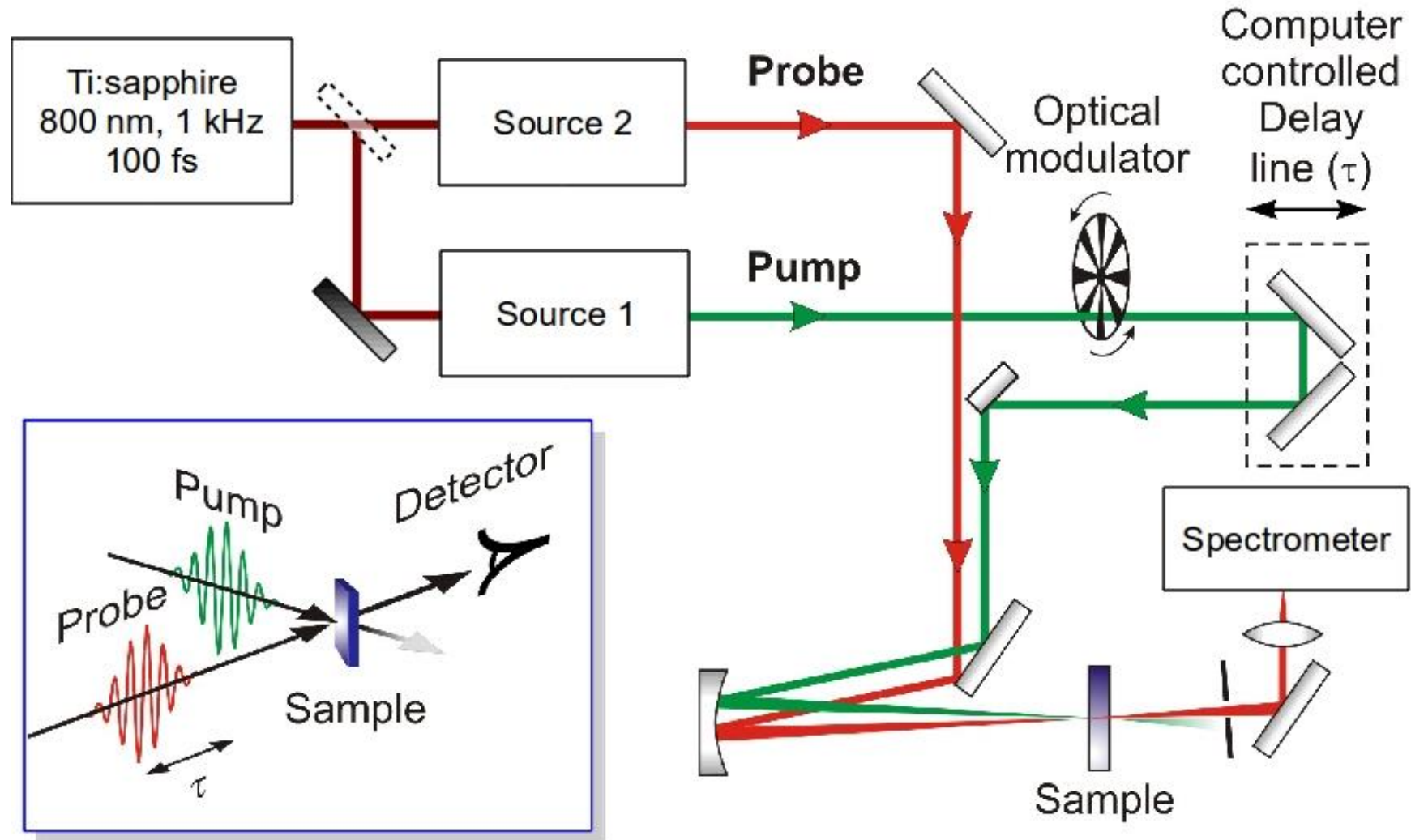
$$k_{sig} = k_1 - k_1 + k_2$$

TRANSIENT ABSORPTION SPECTRA

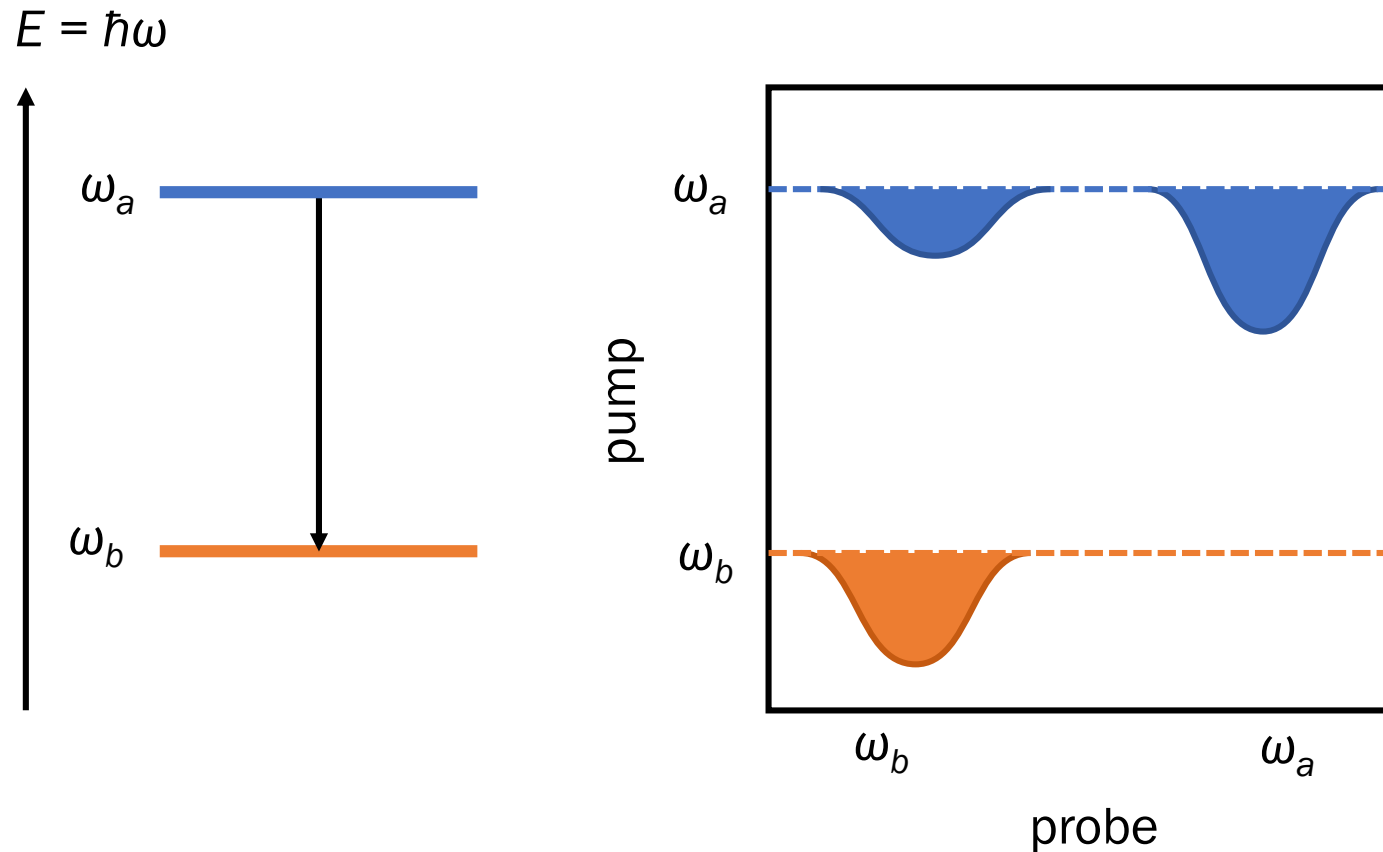


- GSB - ground-state bleaching
- SE - stimulated emission
- ESA - excited-state absorption

EXPERIMENTAL SETUP FOR PUMP-PROBE SPECTROSCOPY



“POOR-MAN” 2D SPECTROSCOPY – DOUBLE RESONANCE



Double resonance experiment (stacked pump-probe spectra)

- Narrowband pump – broadband probe
- The experiment is repeated with varying the pump wavelengths
- The spectra are stacked together to obtain a quasi-2D spectrum

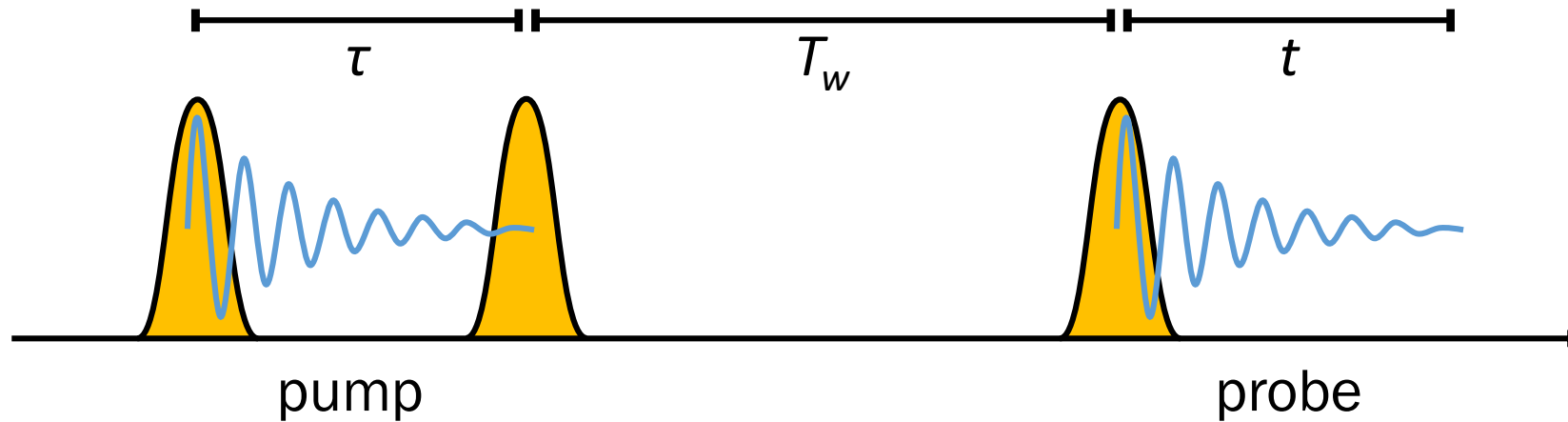
Problems

- Laborious and time consuming (repeated experiments with different excitations)
- Transform limit imposes a trade-off between time and spectral resolution

Solution

- Broadband fourier-transform 2DES

FT 2DES – PULSE SEQUENCE



τ – coherence time

T_w – waiting time

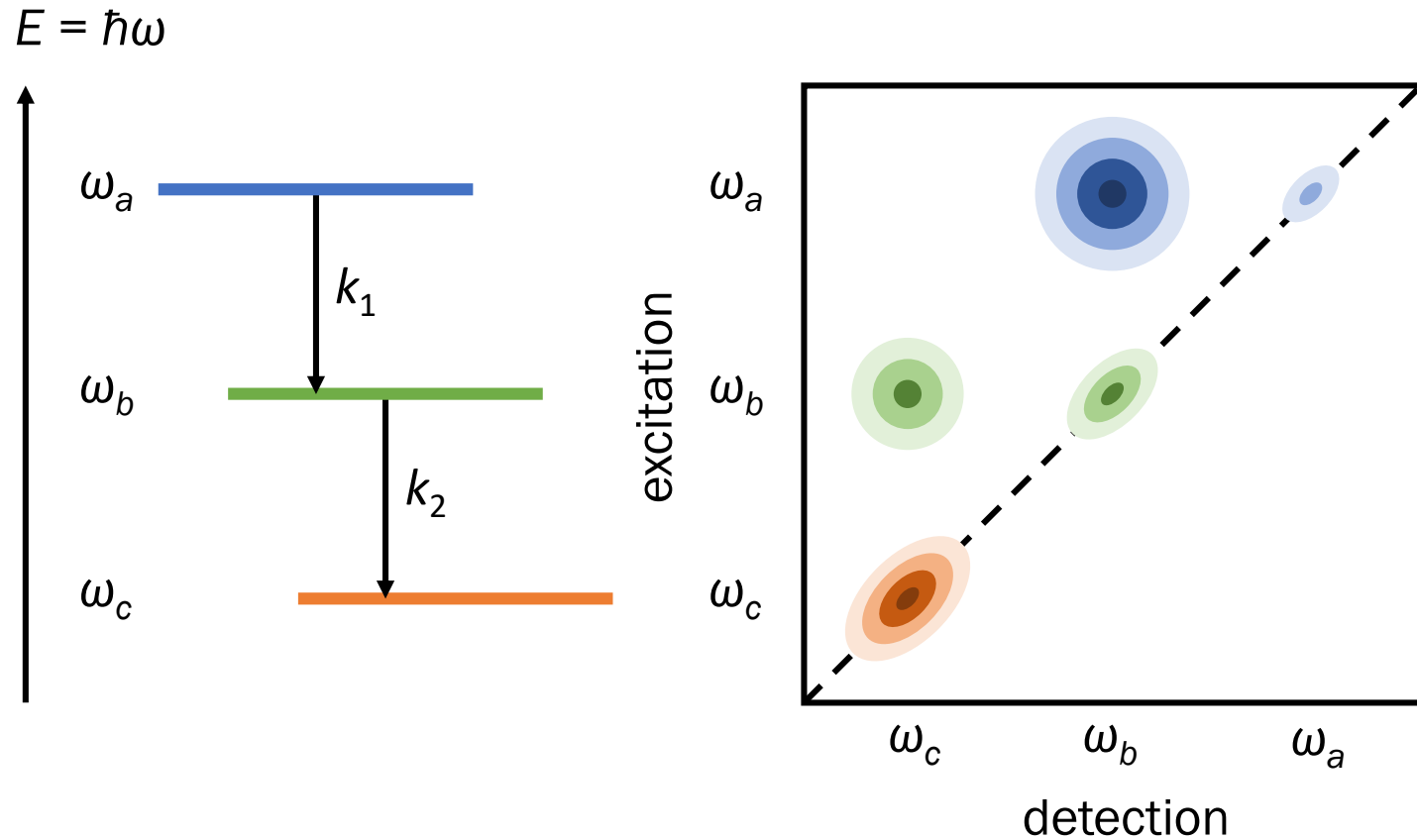
t – detection time

– oscillation frequency ω_τ

– population transfer

– echo signal frequency ω_t

2D ELECTRONIC SPECTRA

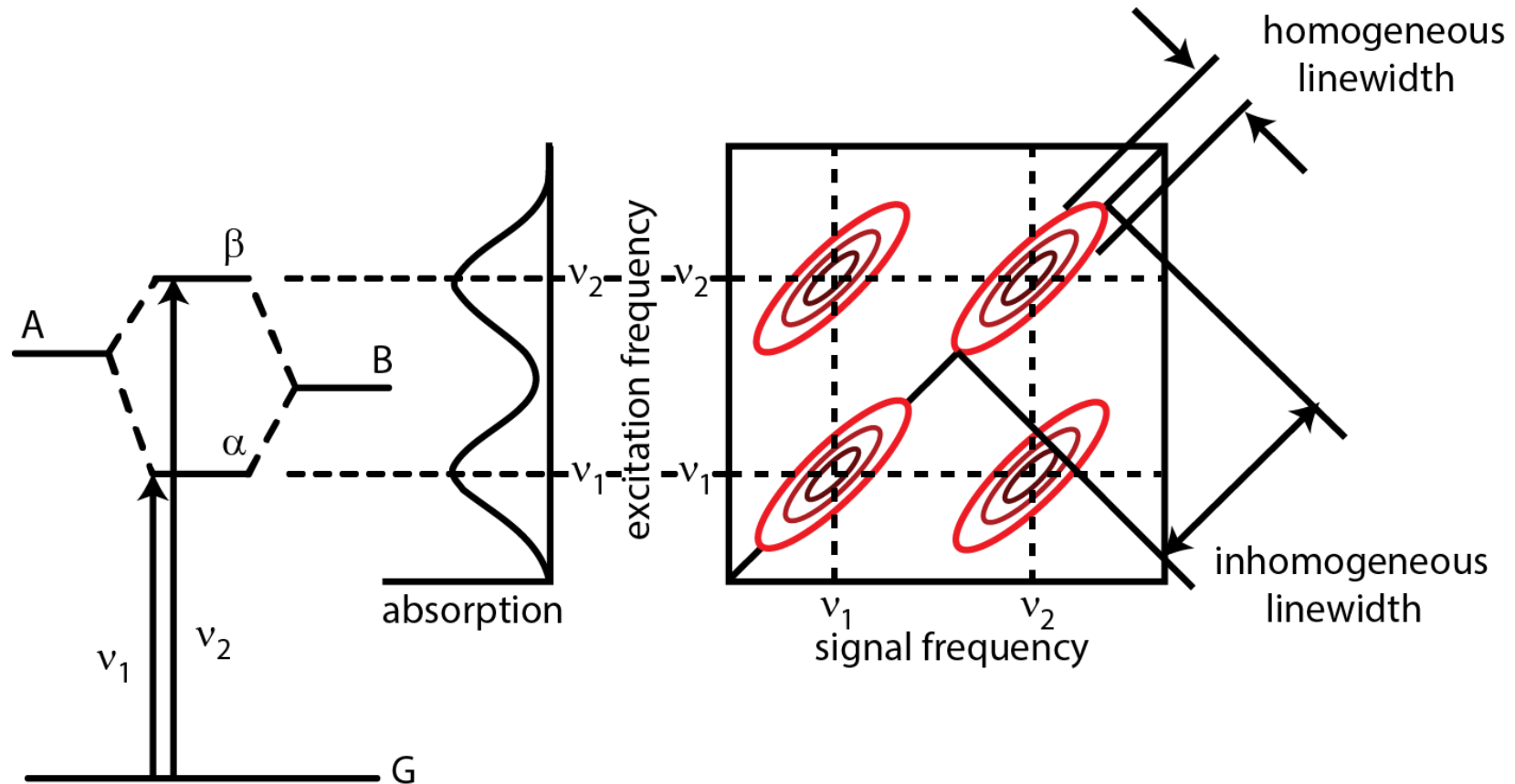


The 2D electronic spectrum

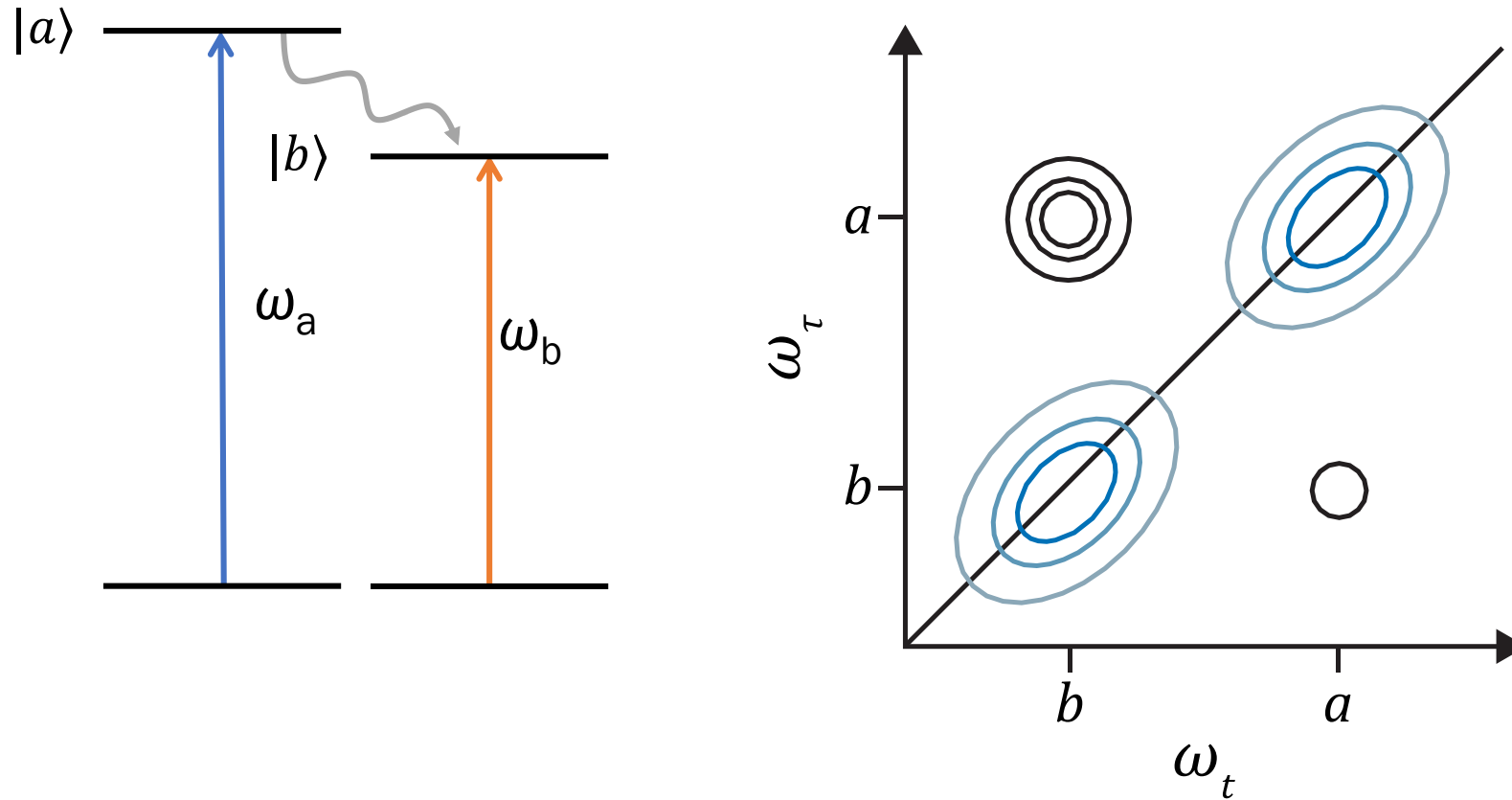
- Is a joint probability:
- The probability to find the system in state Y after excitation of state X
- Diagonal peaks – correspond to bands in the linear absorption spectrum
- Off-diagonal peaks (cross-peaks) show coupling between states

Schematic 2D electronic spectrum of a coupled three-level system

2D ELECTRONIC SPECTROSCOPY – EXCITONIC COUPLING

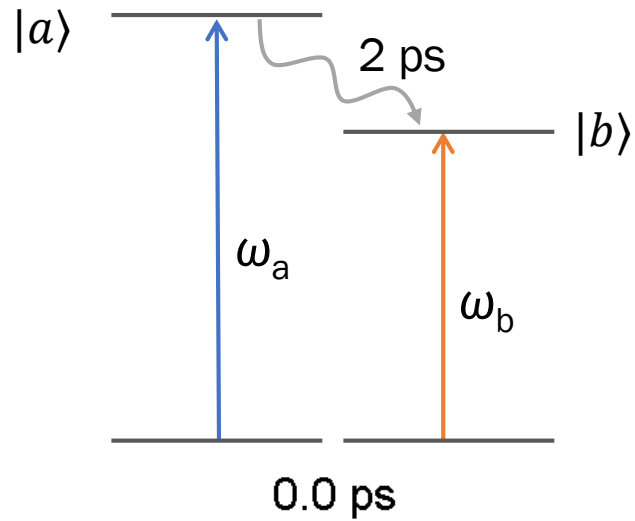


2D ELECTRONIC SPECTROSCOPY – RESOLVING ENERGY TRANSFER

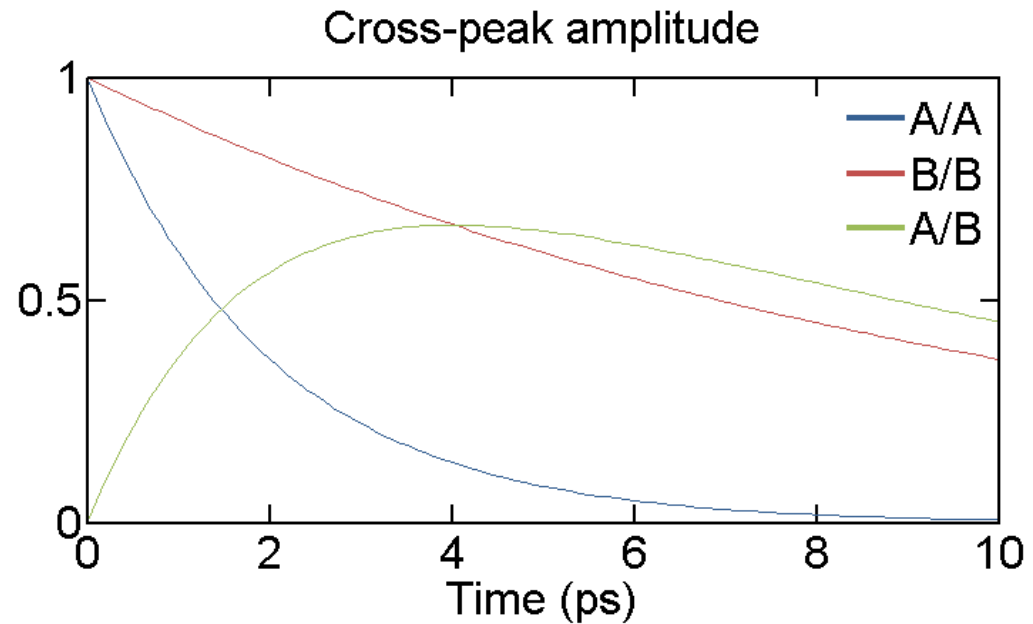
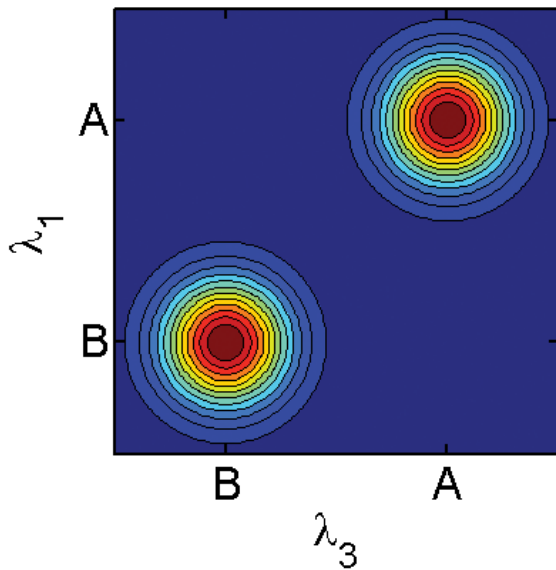


Cross peaks in the 2D spectrum reveal energy transfer

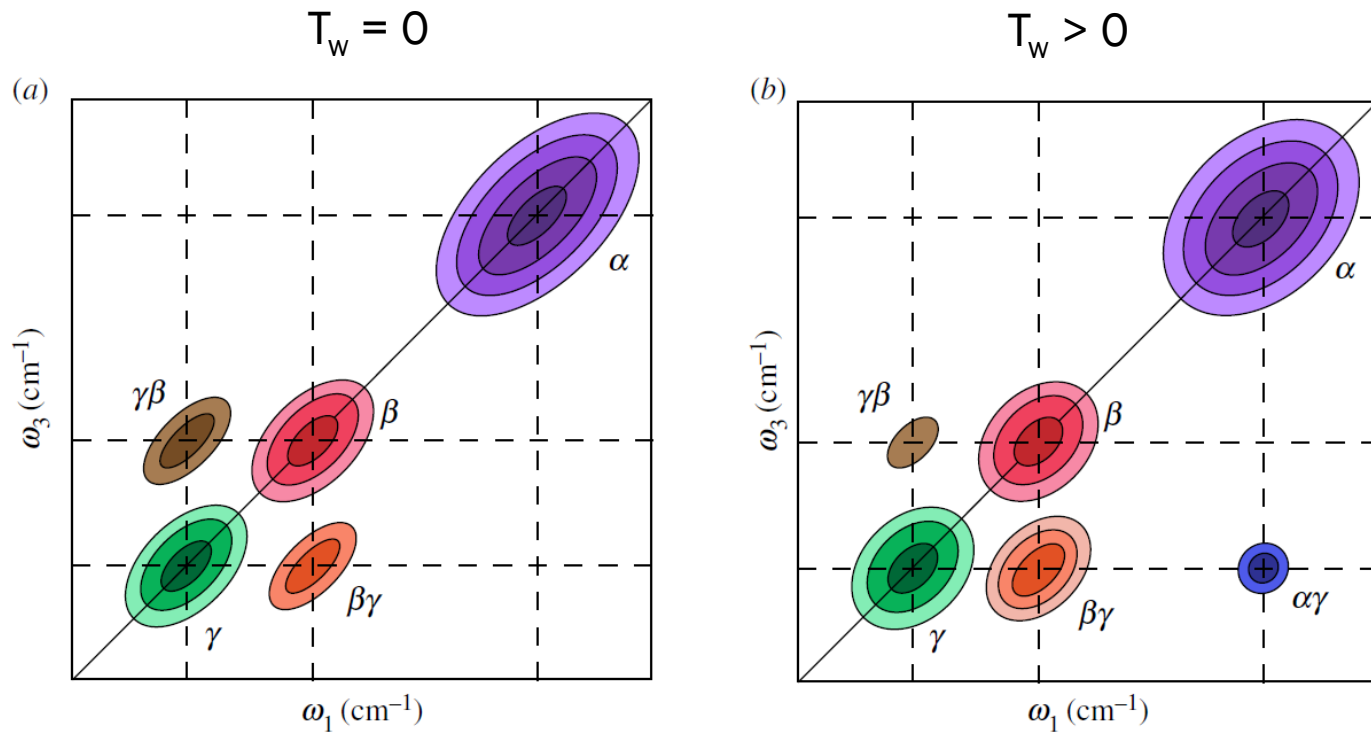
TRANSIENT 2D ELECTRONIC SPECTROSCOPY



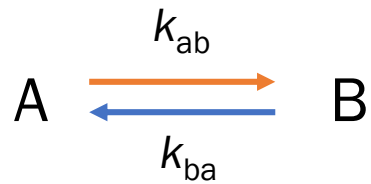
- Cross-peak at $(\lambda_1 = A, \lambda_3 = B)$ reflects energy transfer from $|a\rangle$ to $|b\rangle$
- $\lambda_1 = A$ - donor's Abs wavelength
- $\lambda_3 = B$ - acceptor's Abs wavelength



EXCITONIC COUPLING AND ENERGY TRANSFER

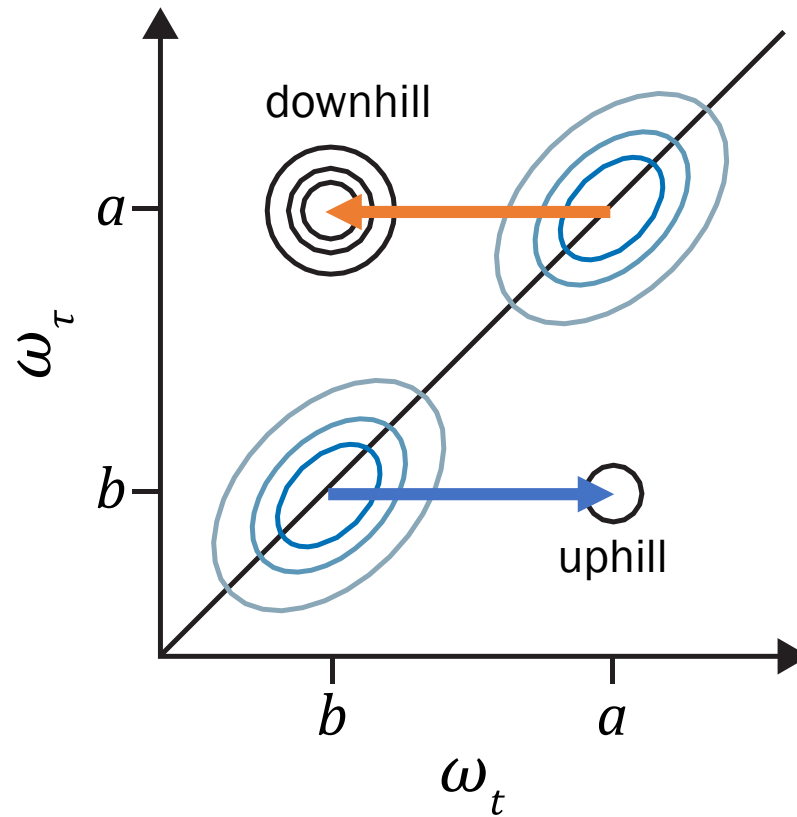


DOWNHILL VS UPHILL ENERGY TRANSFER



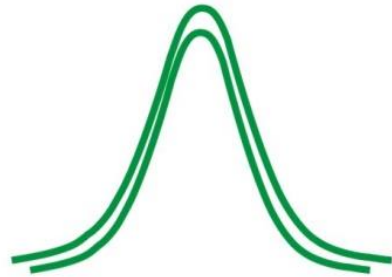
$$\frac{k_{ab}}{k_{ba}} = e^{-\frac{\Delta E}{k_B T}}$$

Detailed balance
(Boltzmann distribution)

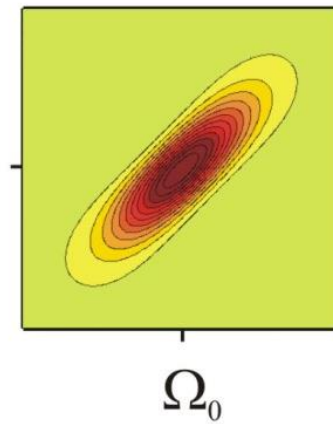
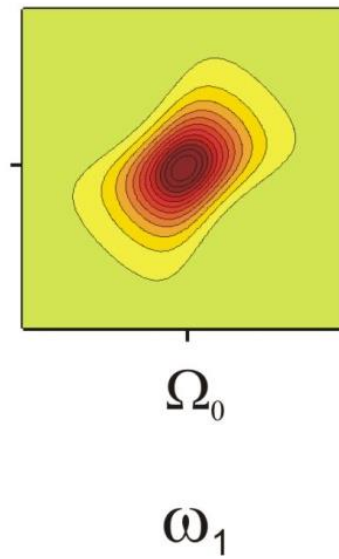
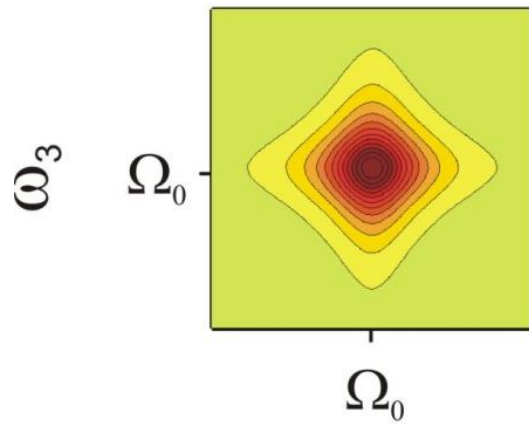
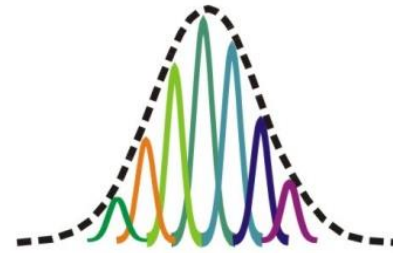
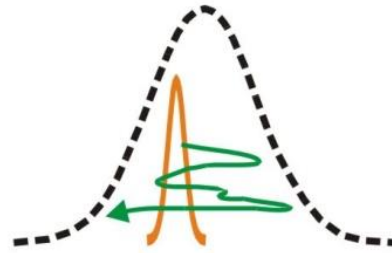


2D LINESHAPES

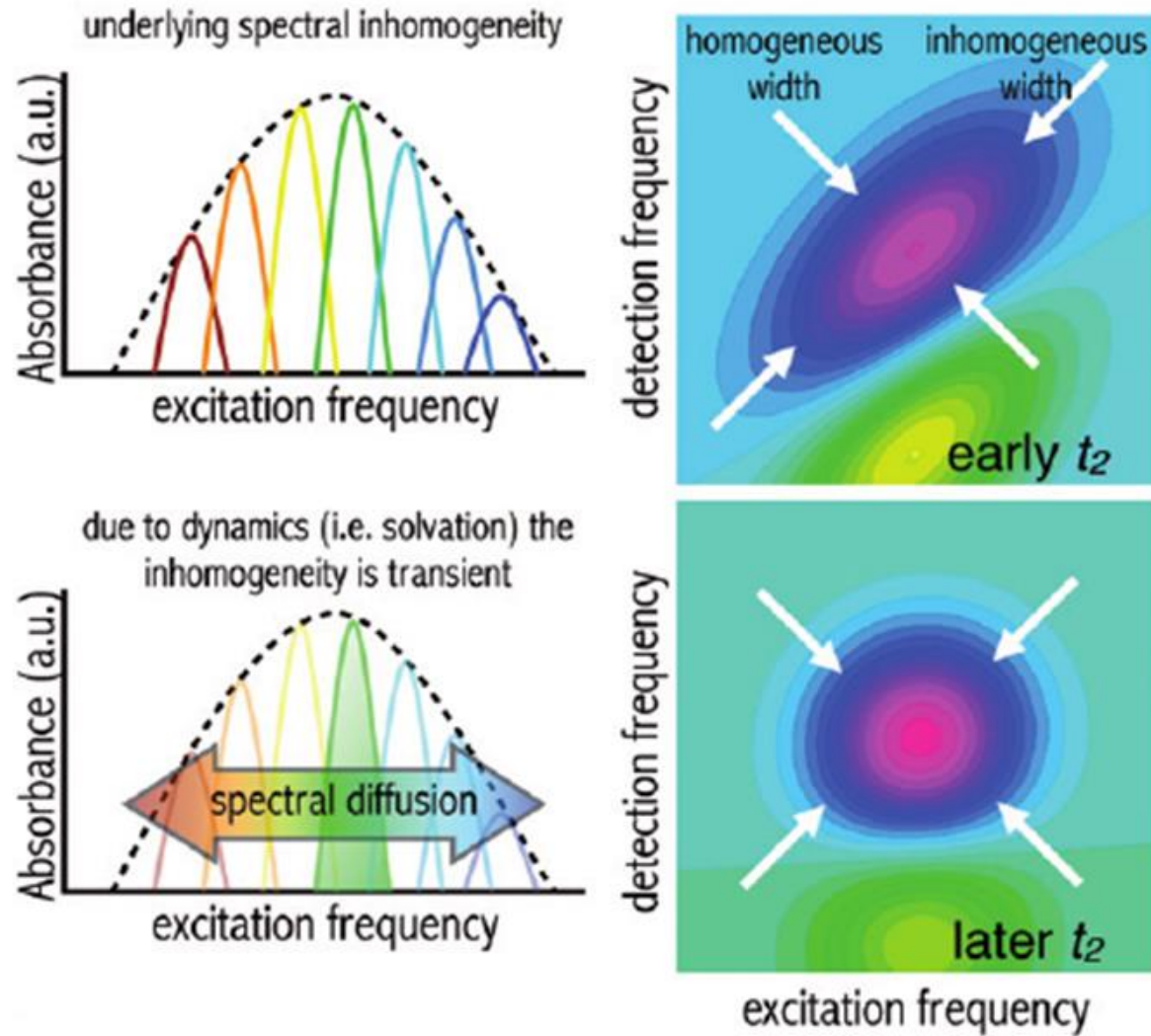
Homogeneous



Inhomogeneous

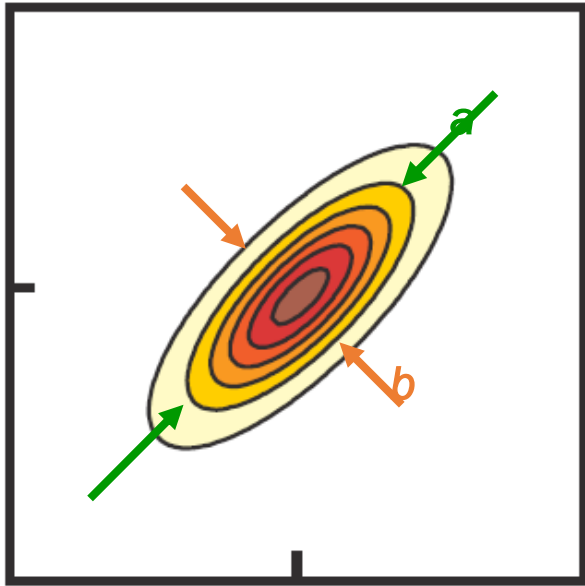


SPECTRAL BROADENING AND SPECTRAL DIFFUSION

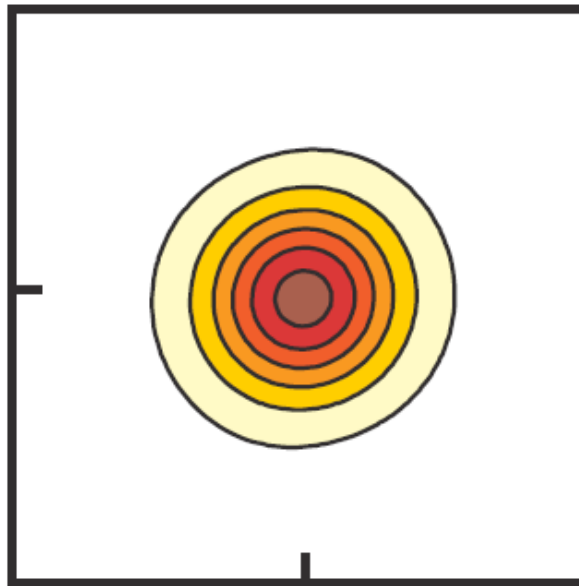


2D LINESHAPES: LOSS OF FREQUENCY CORRELATION

$$\tau_2 \ll \tau_c$$



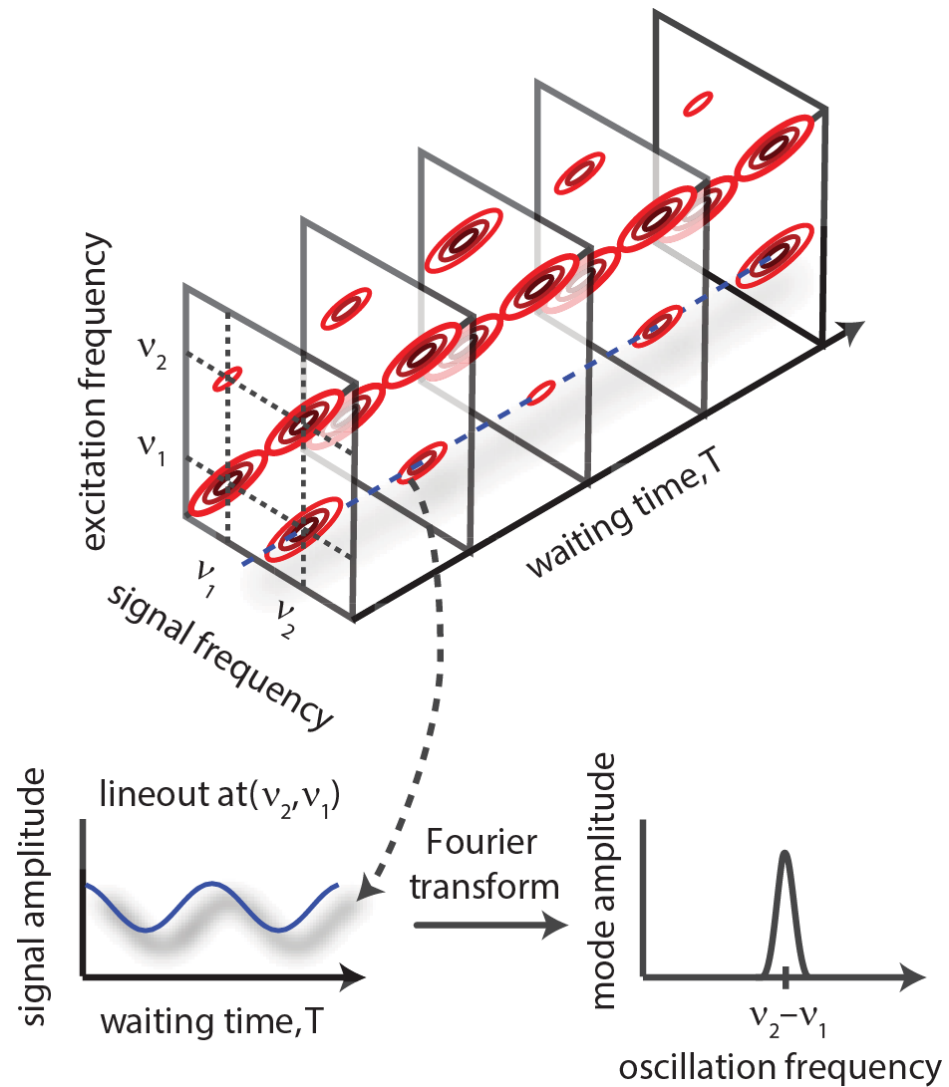
$$\tau_2 \gg \tau_c$$



Ellipticity

$$E = \frac{a^2 - b^2}{a^2 + b^2}$$

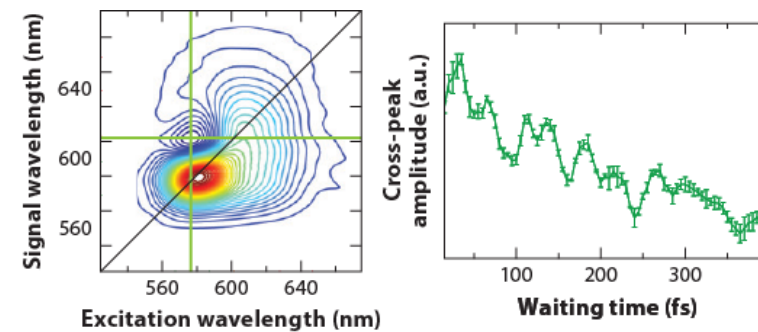
COHERENT DYNAMICS



Exciton coherence:

- Coherent superposition of eigenstates
- Cross-peaks oscillate with T_w
- The oscillation frequency reflects the energy split

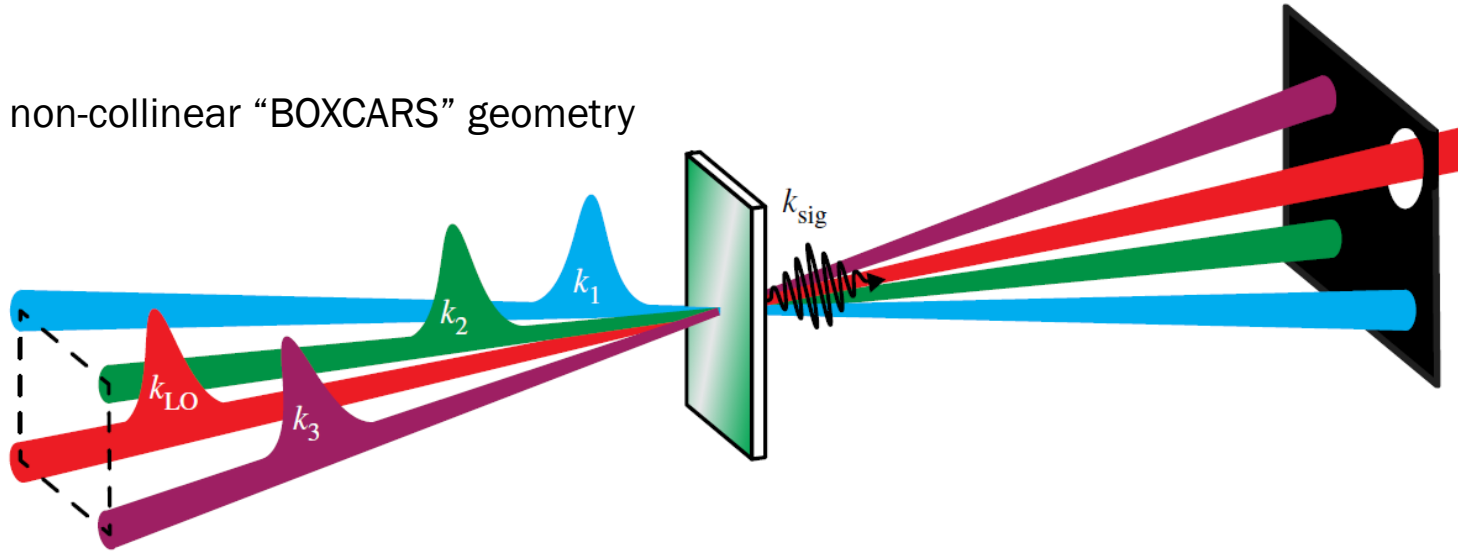
Coherence dynamics in PC645



TECHNICAL IMPLEMENTATIONS

TECHNICAL IMPLEMENTATIONS OF 2DES

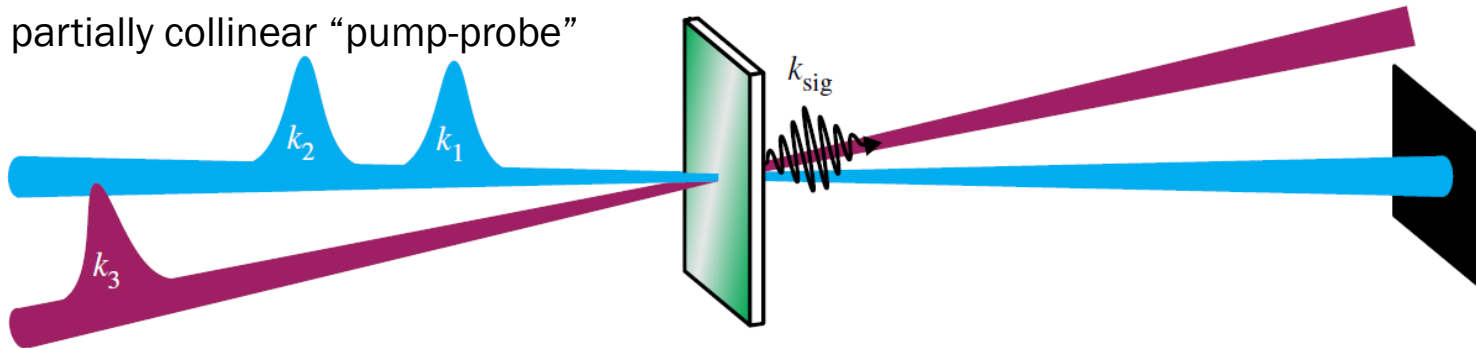
non-collinear "BOXCARS" geometry



BOXCARS geometry

- ✓ Background-free
- ✓ Signals of interest detected in the phase-matching direction
- ✓ Separation of rephasing/non-rephasing signal
- ✓ Full polarization control possible
- ✗ The absorptive signal is a sum of two experiments (phasing issues)

partially collinear "pump-probe" geometry

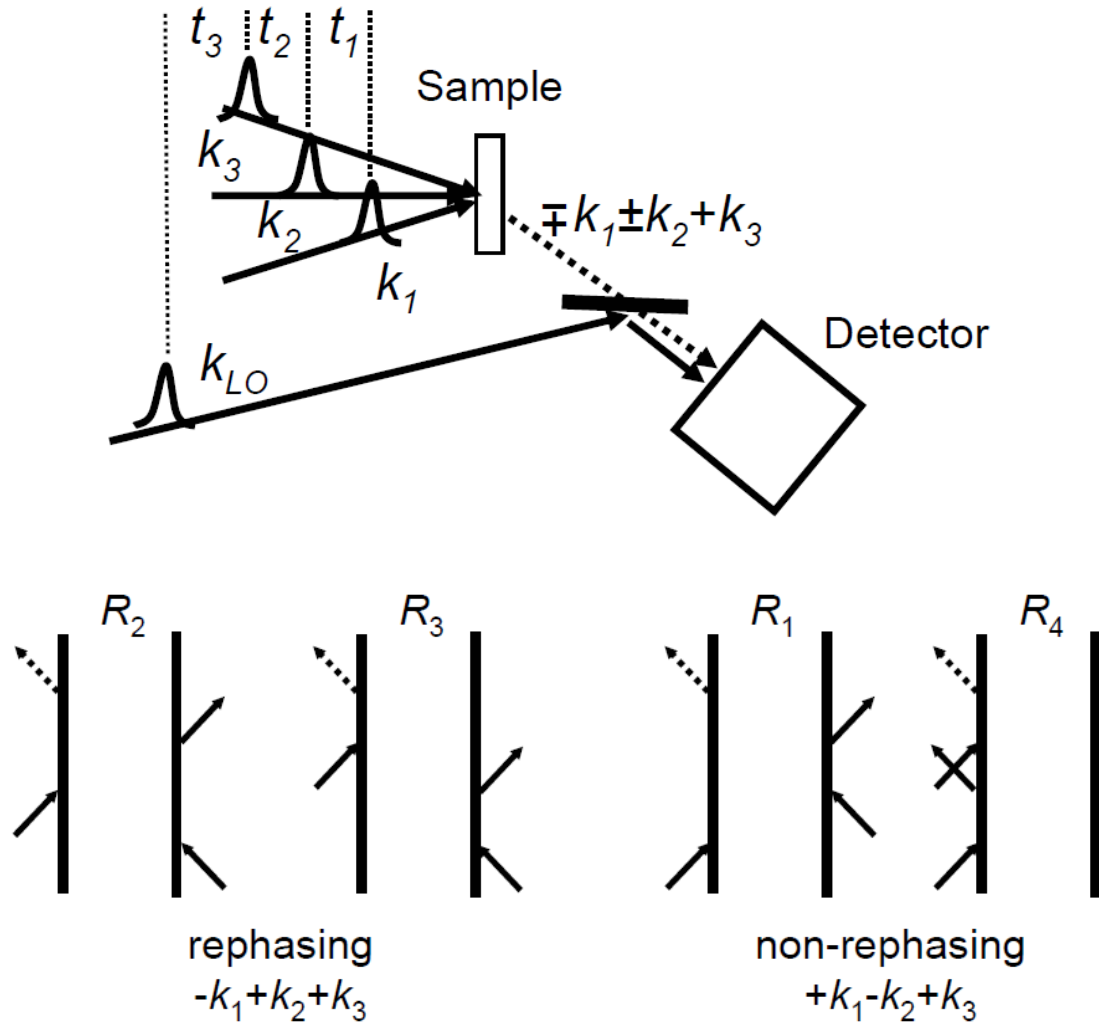


Pump-probe geometry

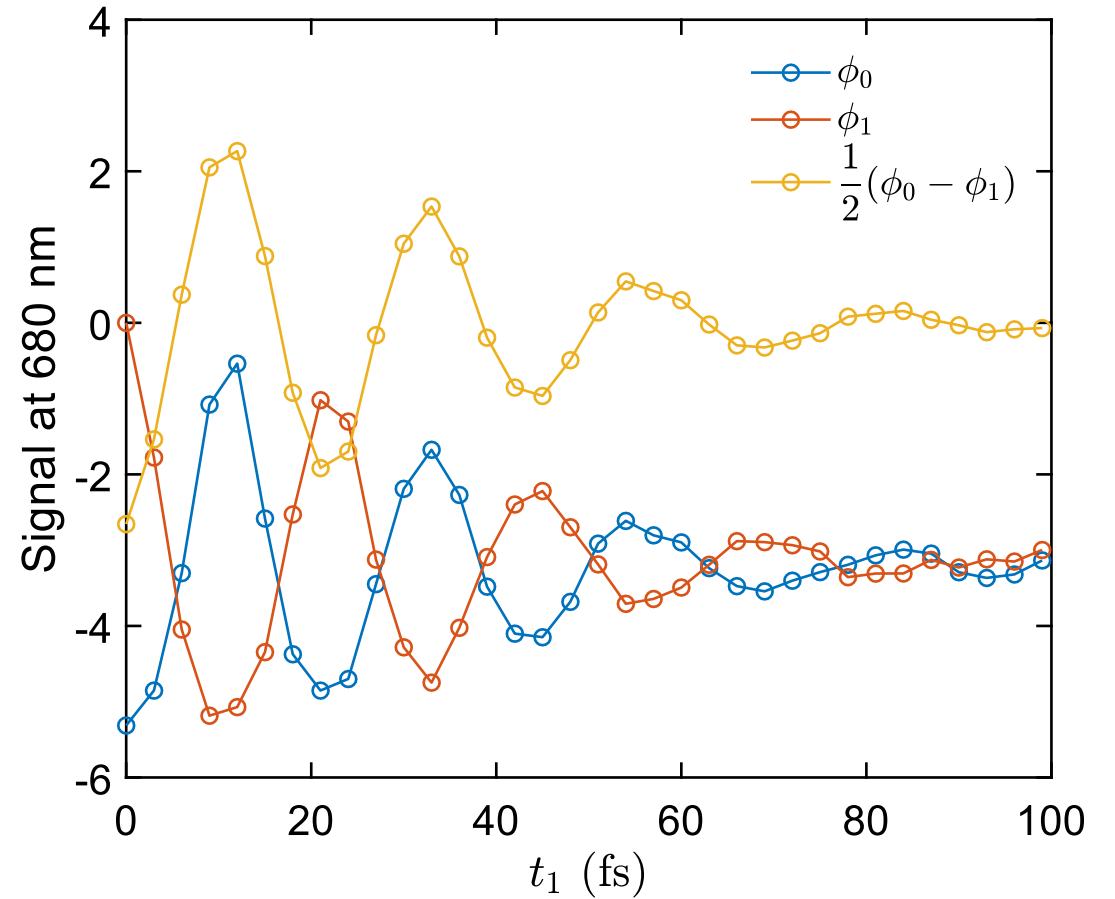
- ✗ The signal and background (probe) are collinear
- ✗ No full polarization control
- ✓ Signal isolated by phase cycling
- ✓ Simpler setup
- ✓ Less data points (partial RF)
- ✓ Absorptive shape, no phase error

PHASE MATCHING VS PHASE CYCLING

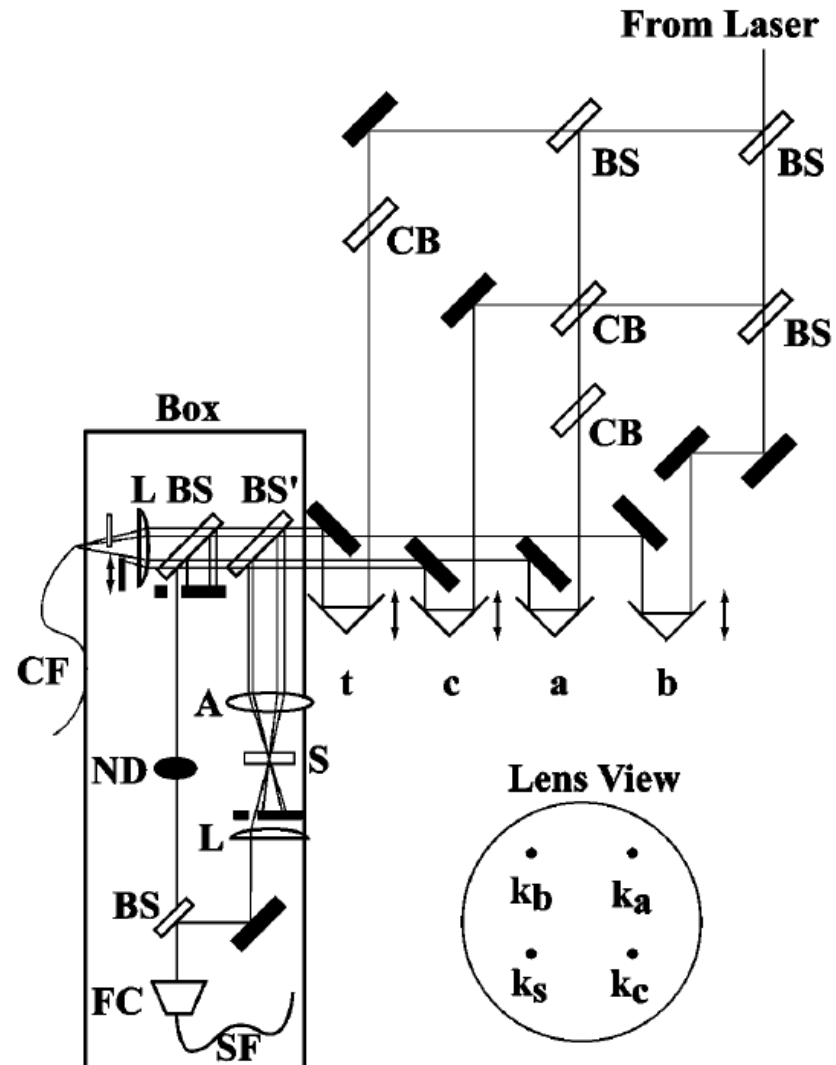
Phase matching (BOXCARS)



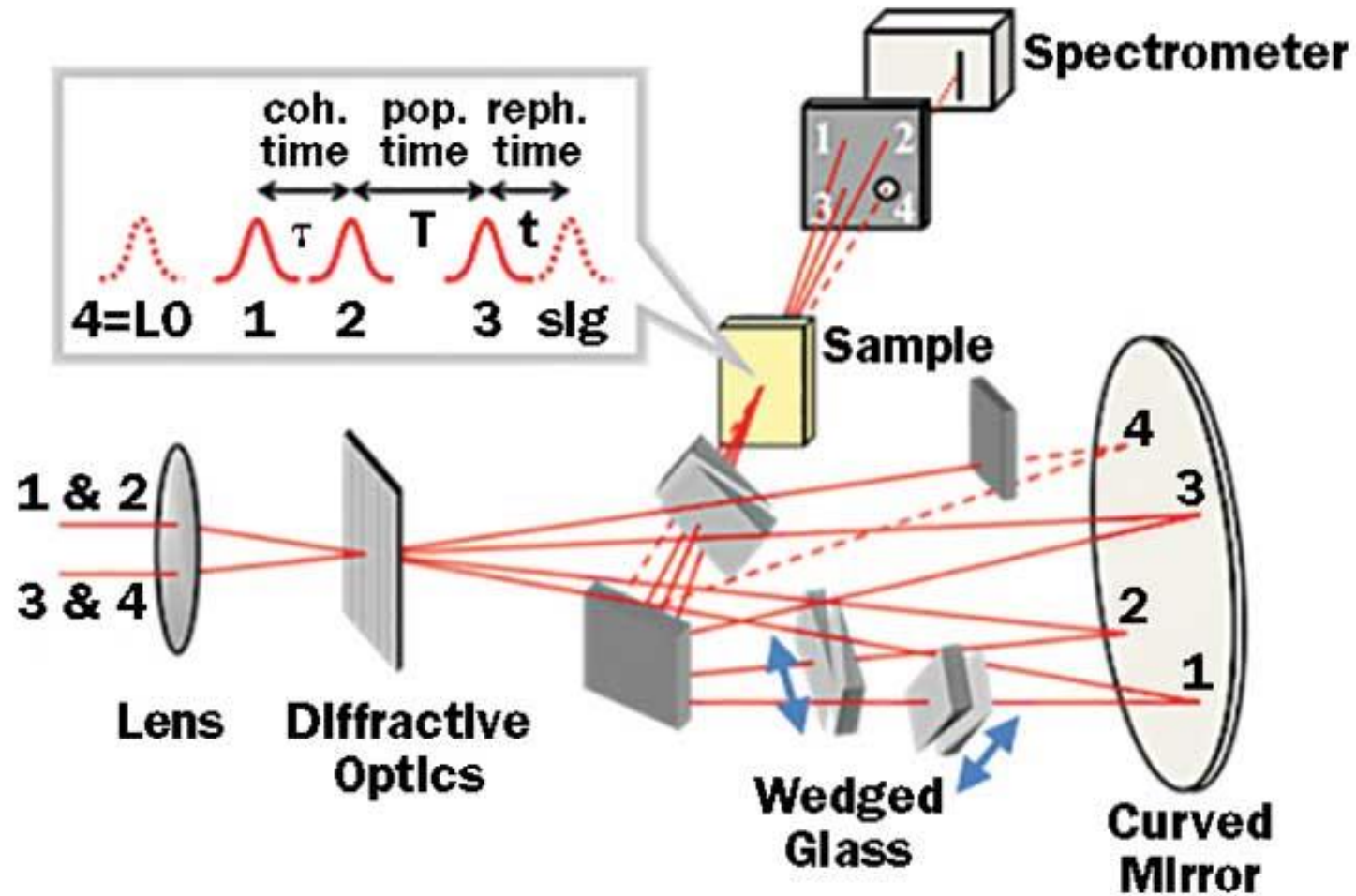
Phase cycling (Pump-probe geometry)



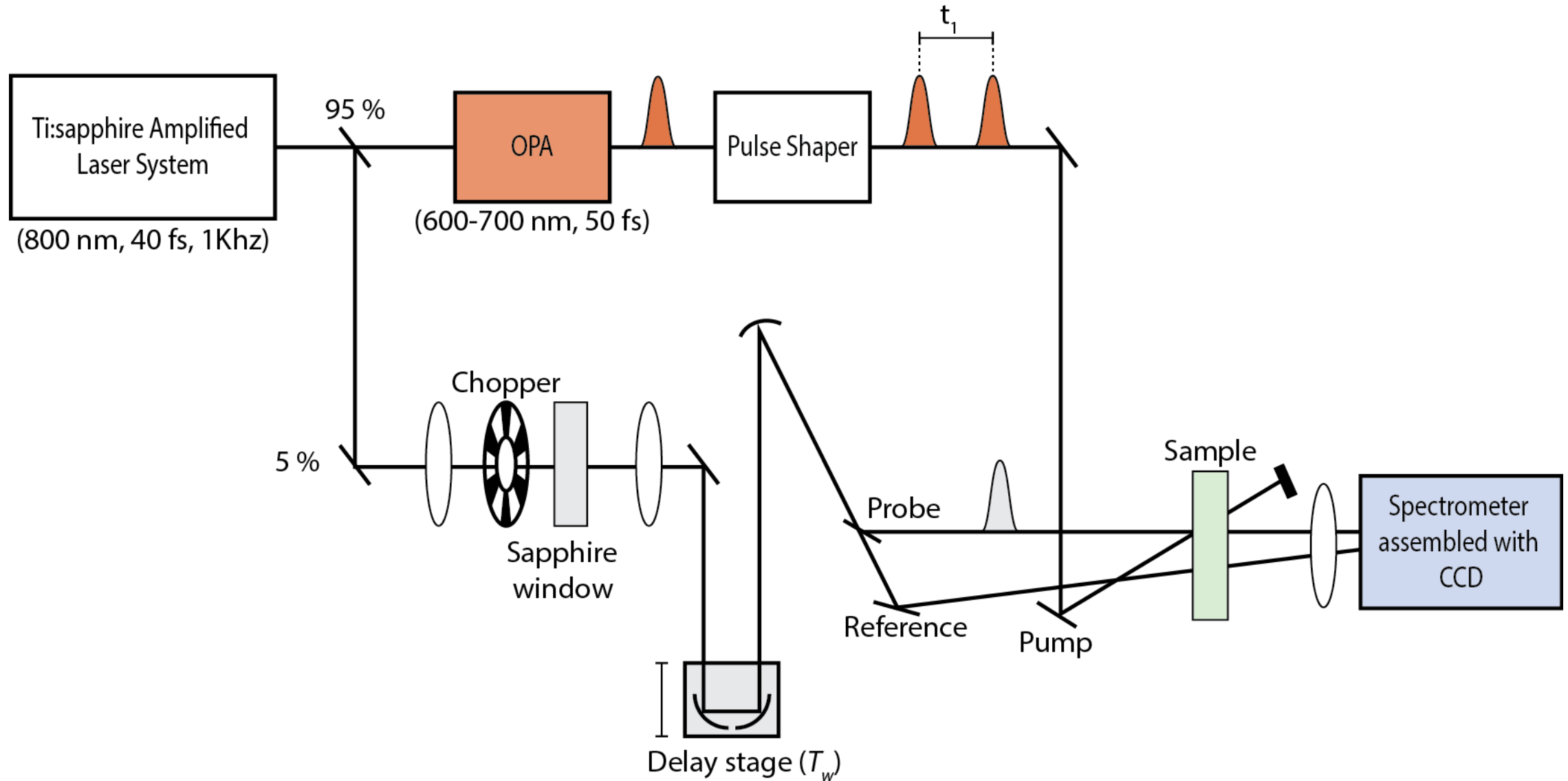
INTERFEROMETER-BASED BOXCARS SETUP



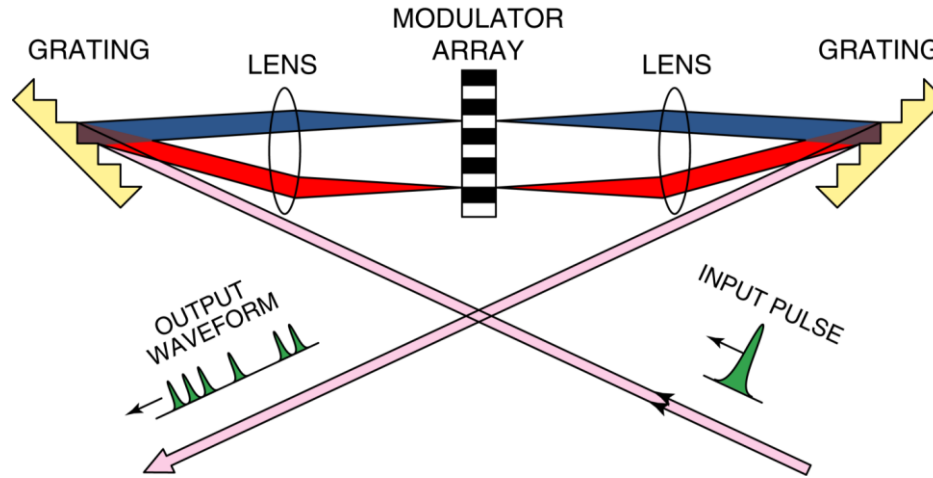
BOXCARS SETUP USING DIFFRACTIVE OPTICS



PULSE-SHAPER-ASSISTED PUMP-PROBE GEOMETRY SETUP

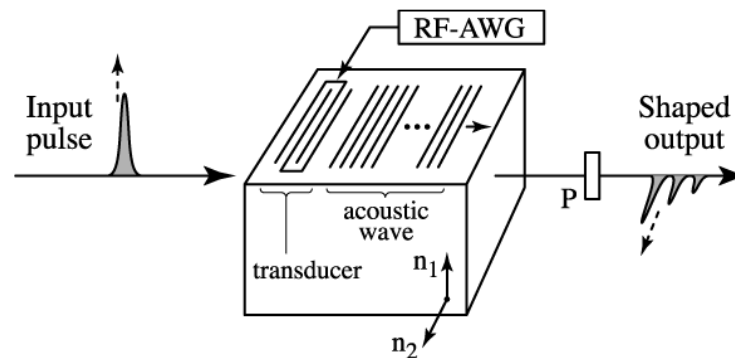


FT PULSE SHAPING



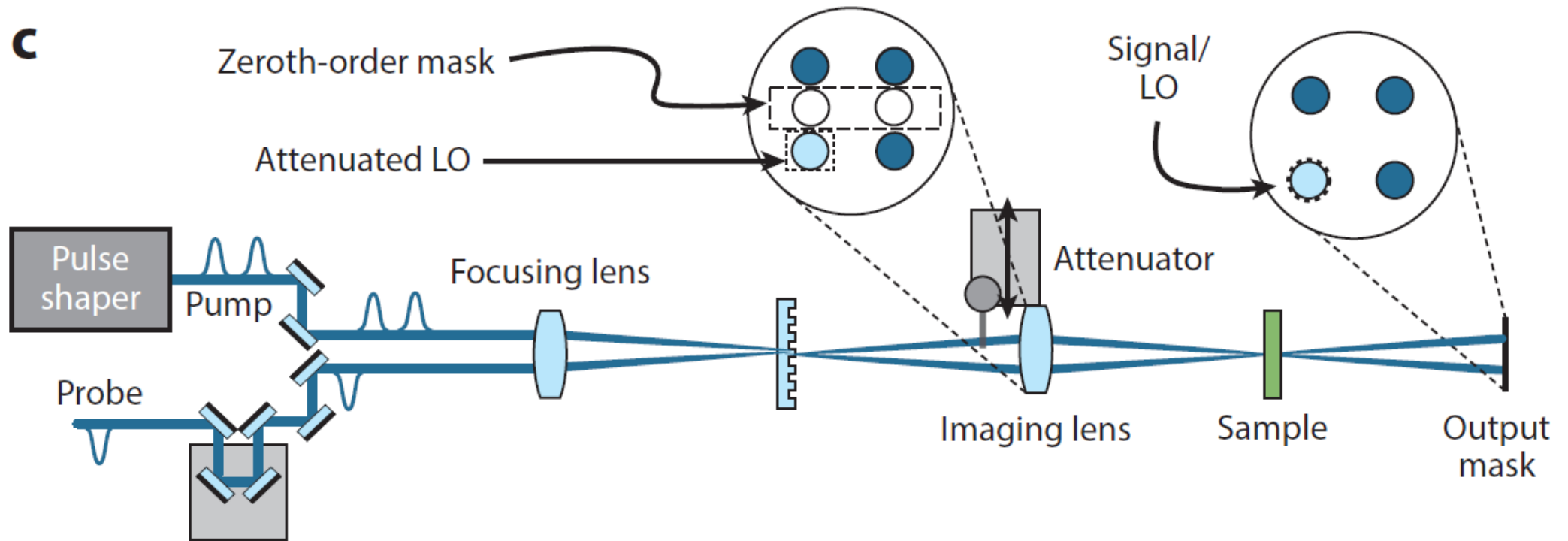
Fourier synthesis via parallel spatial/spectral modulation

Variety of spatial light modulators (SLM): LCD, LCM, deformable mirrors, AOM

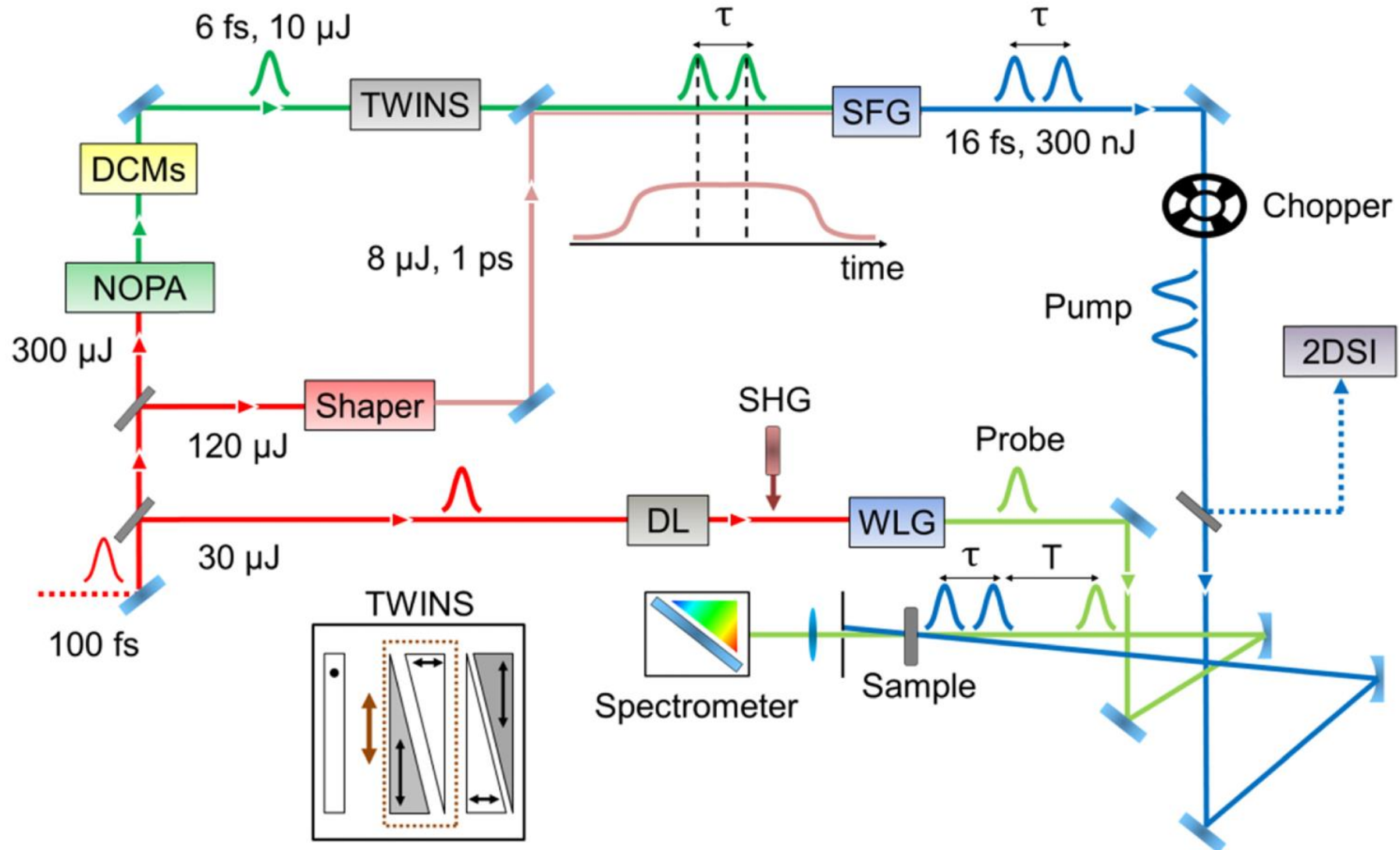


Acousto-optic Programmable Dispersive Filter (AOPDF)

HYBRID PULSE-SHAPER-DO SETUP

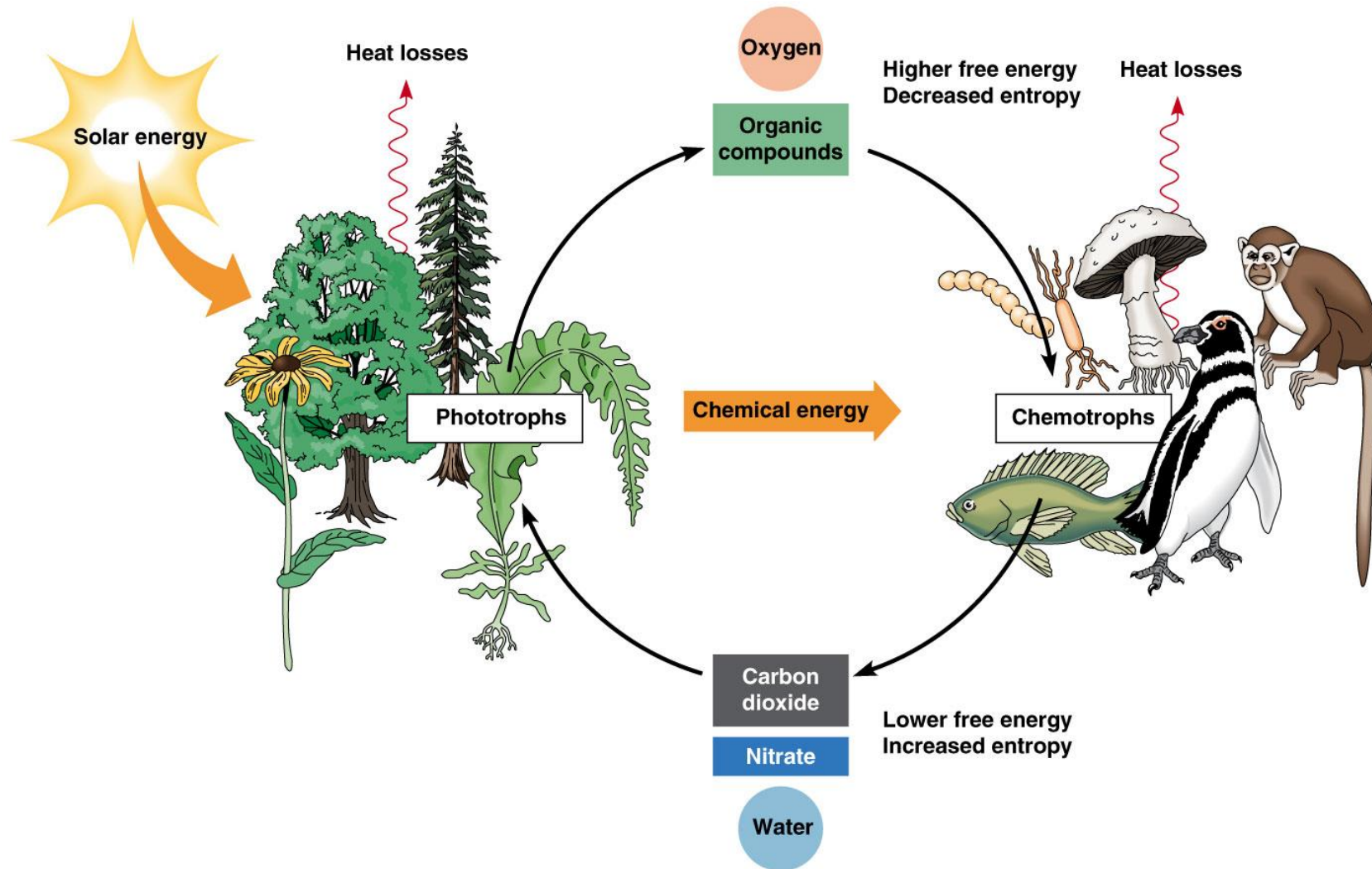


TRANSLATING WEDGE INTERFEROMETER (TWINS) SETUP

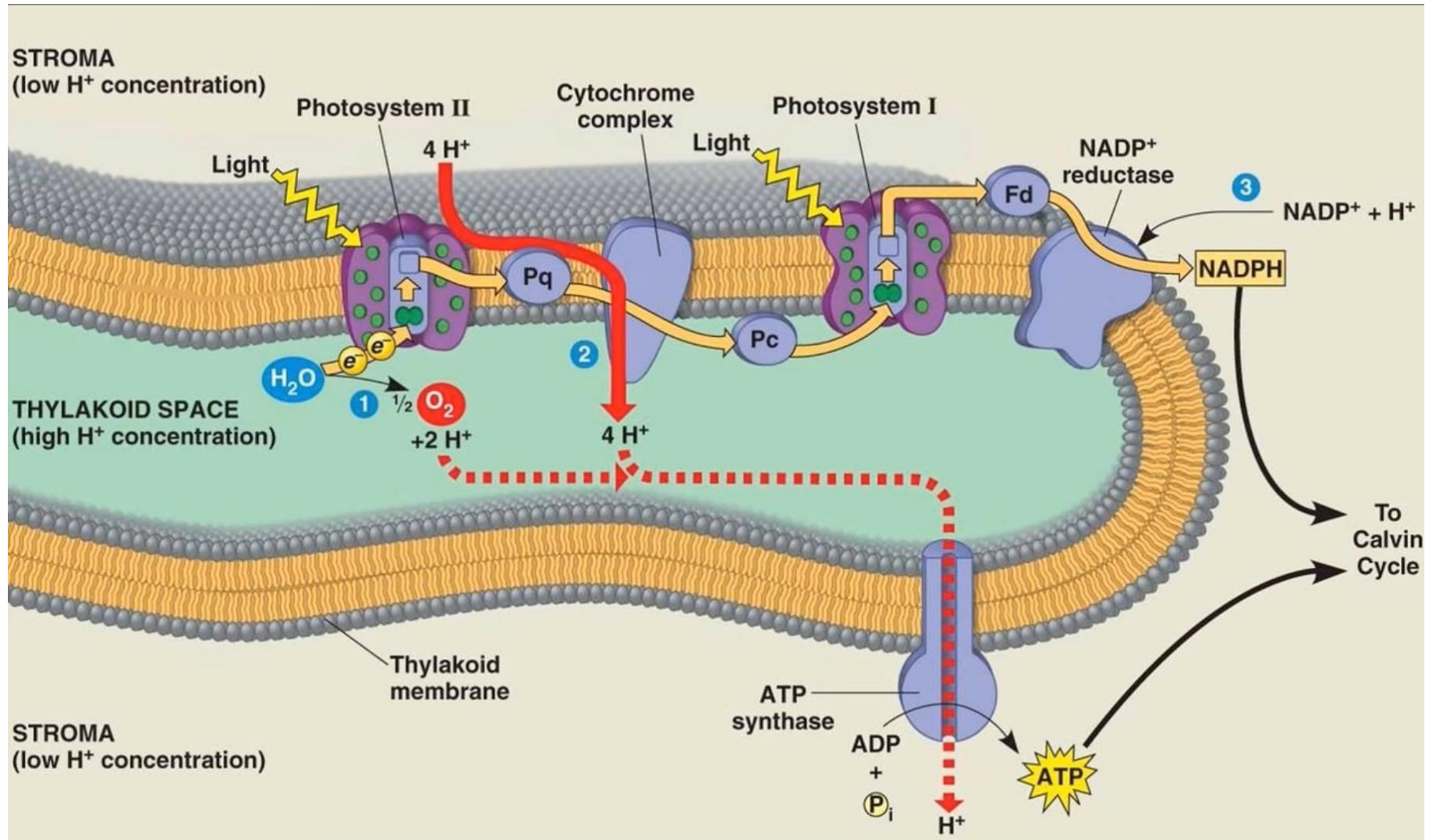


APPLICATIONS IN PHOTOSYNTHESIS

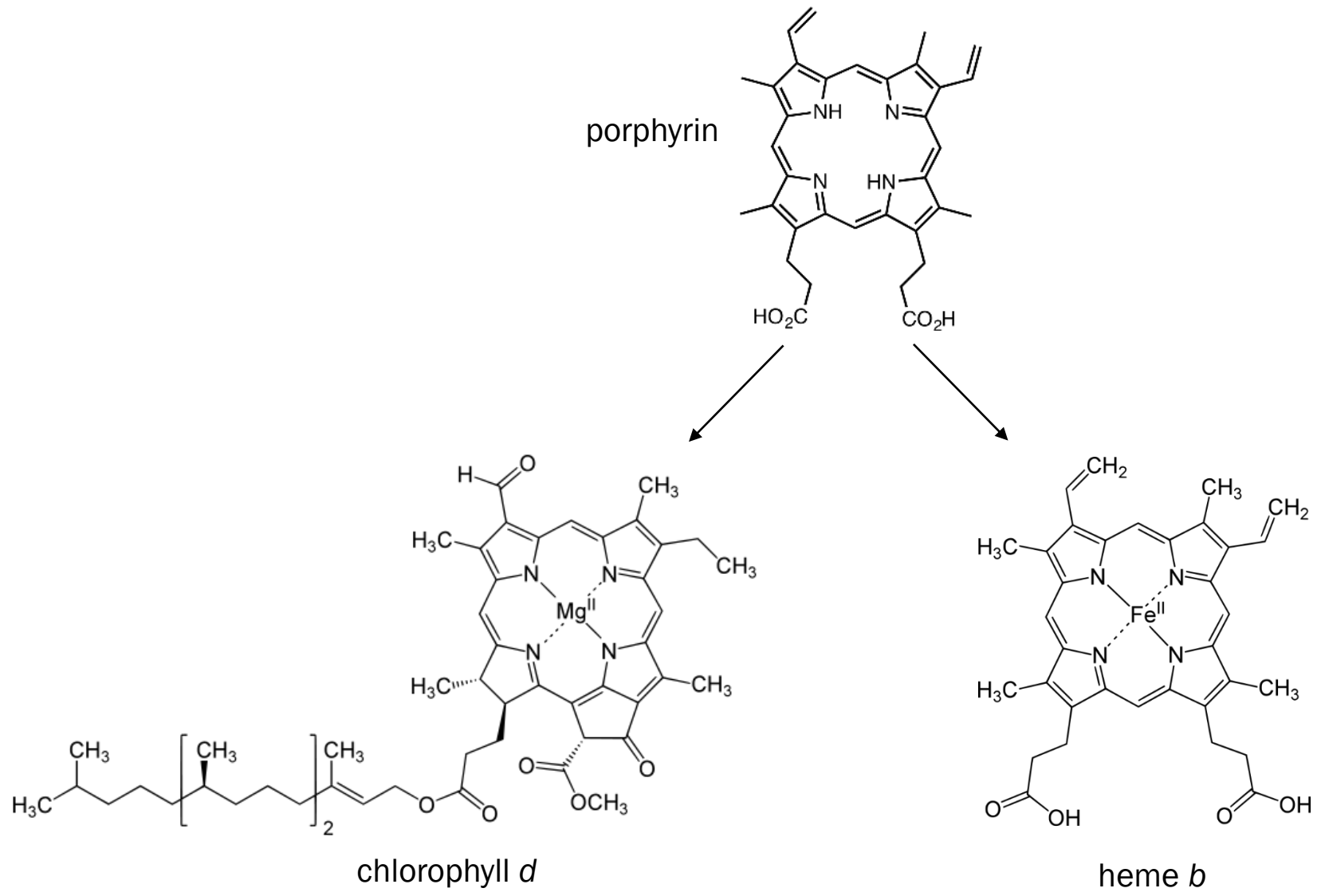
PHOTOSYNTHESIS POWERS LIFE



PHOTOSYNTHETIC ELECTRON TRANSPORT

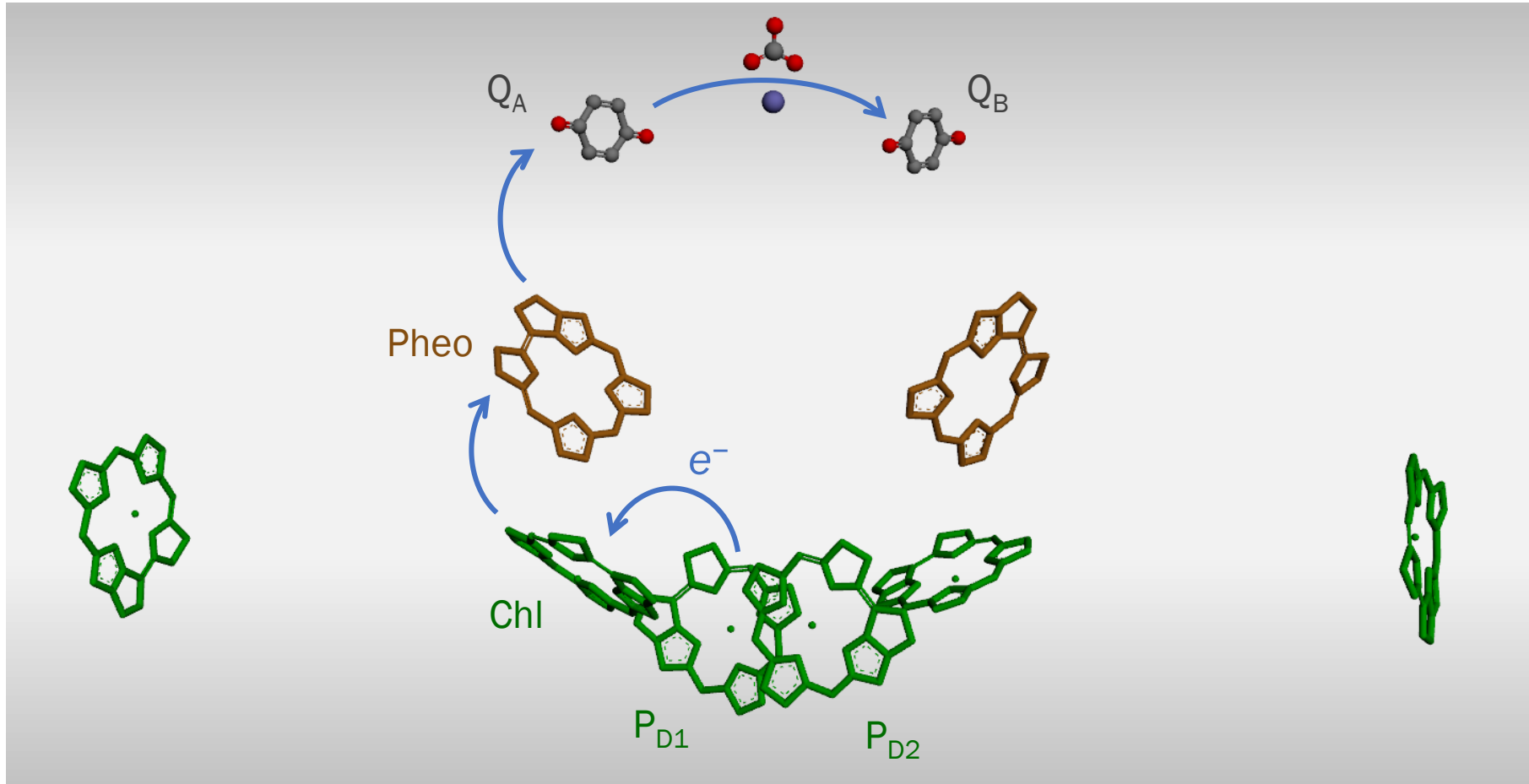


CHLOROPHYLL STRUCTURE



PHOTOCHEMISTRY OCCURS IN THE REACTION CENTRE

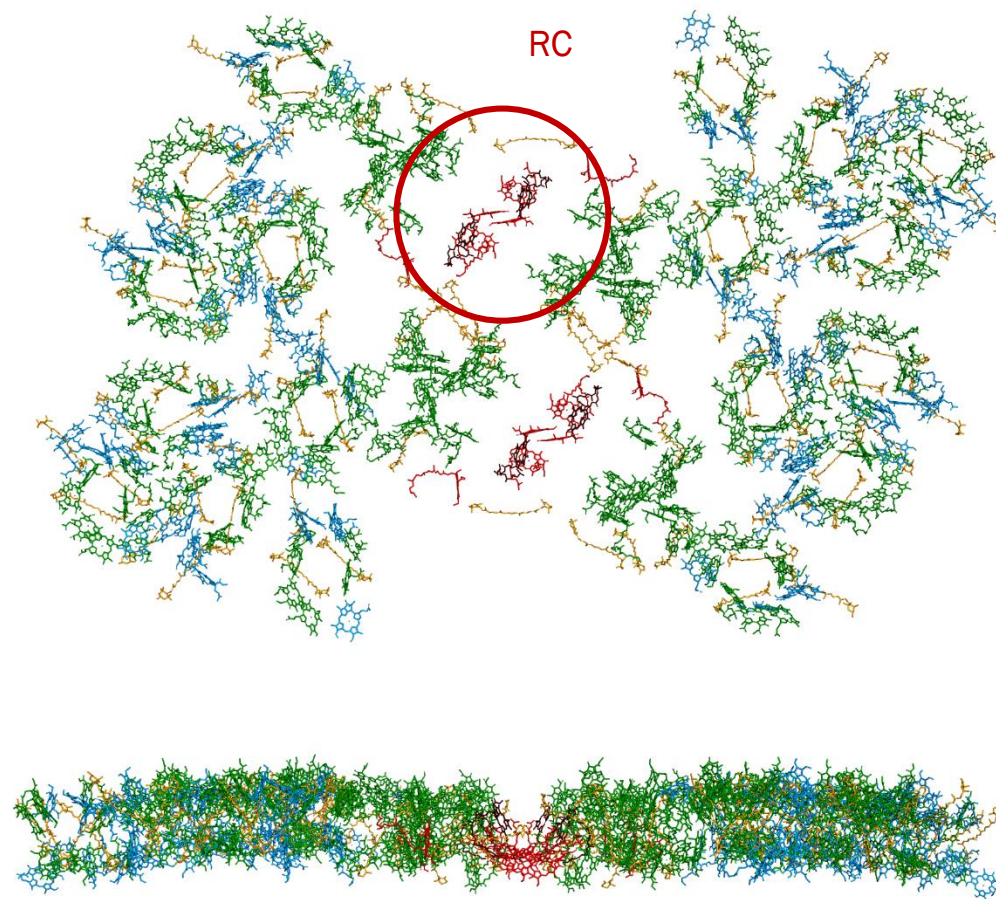
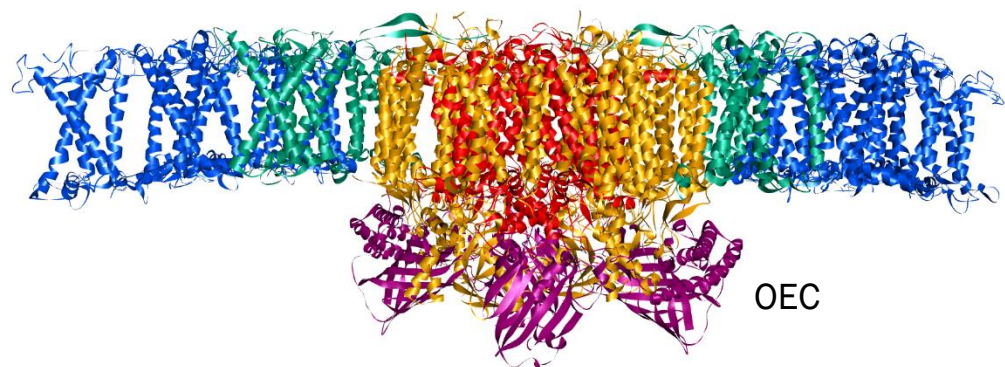
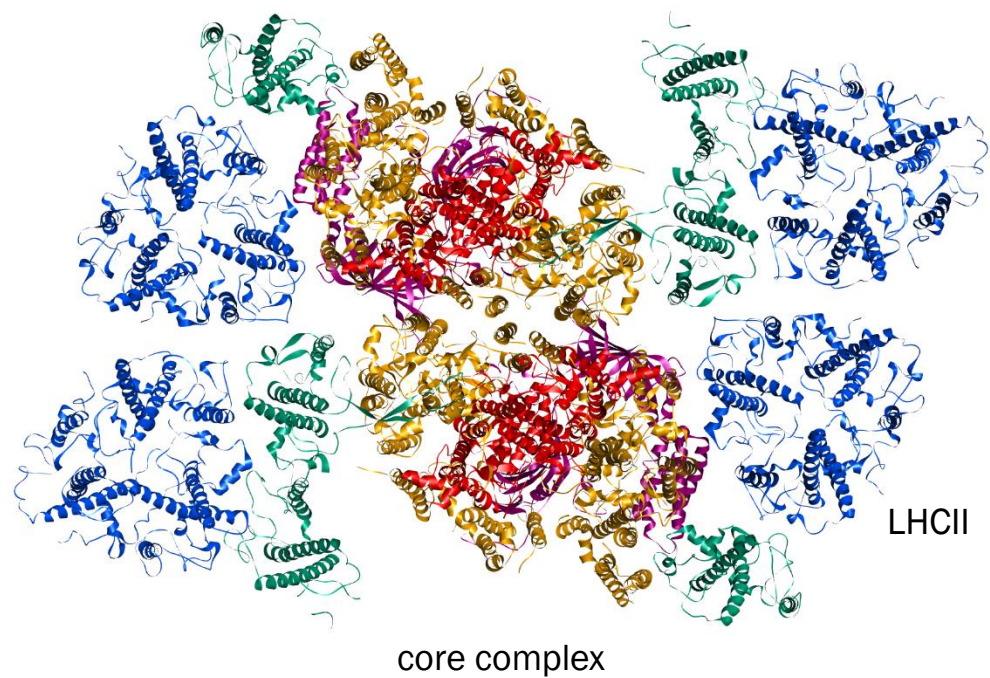
stroma



thylakoid space

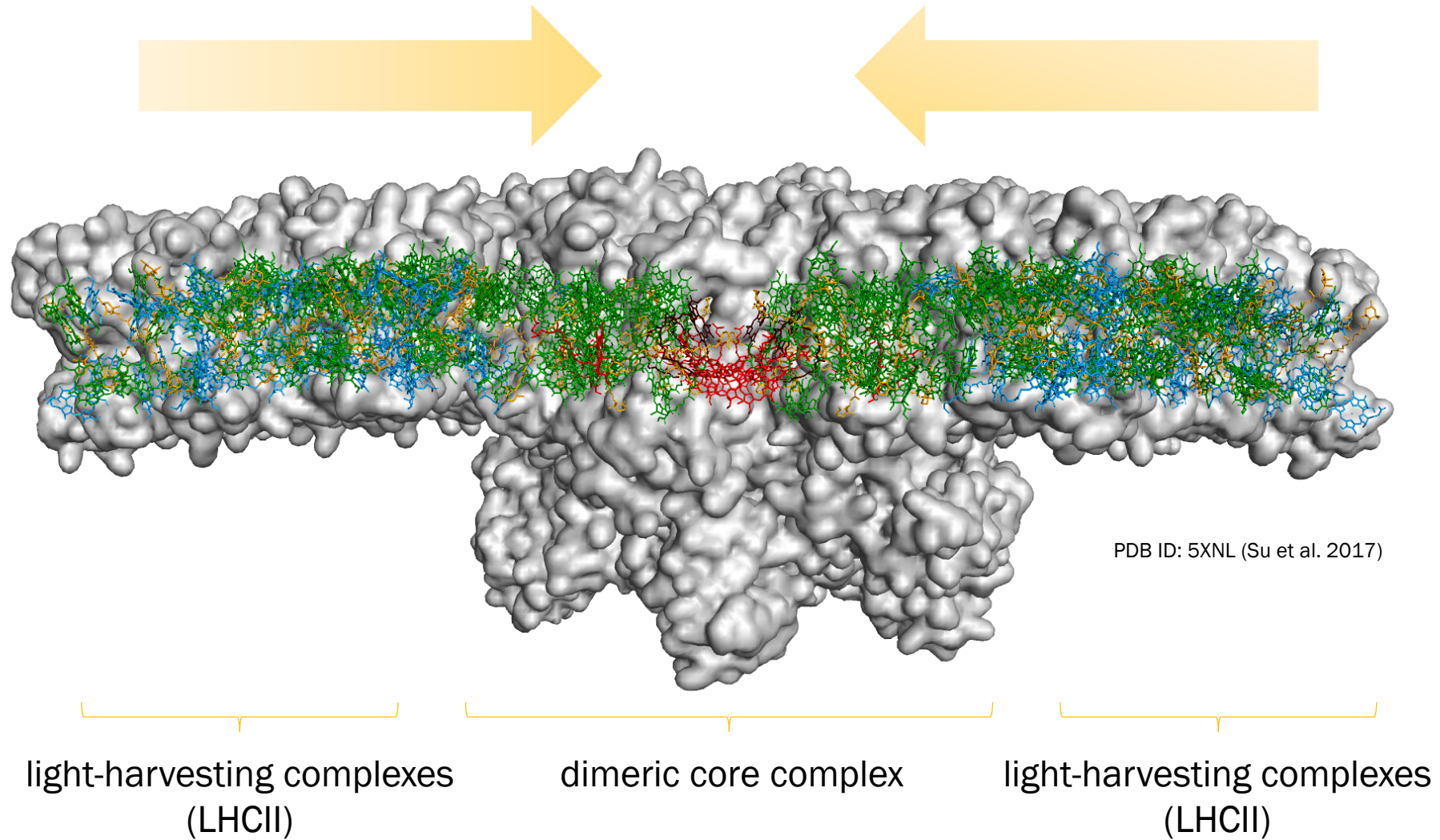
Photosystem II reaction centre

THE PSII-LHCII SUPERCOMPLEX

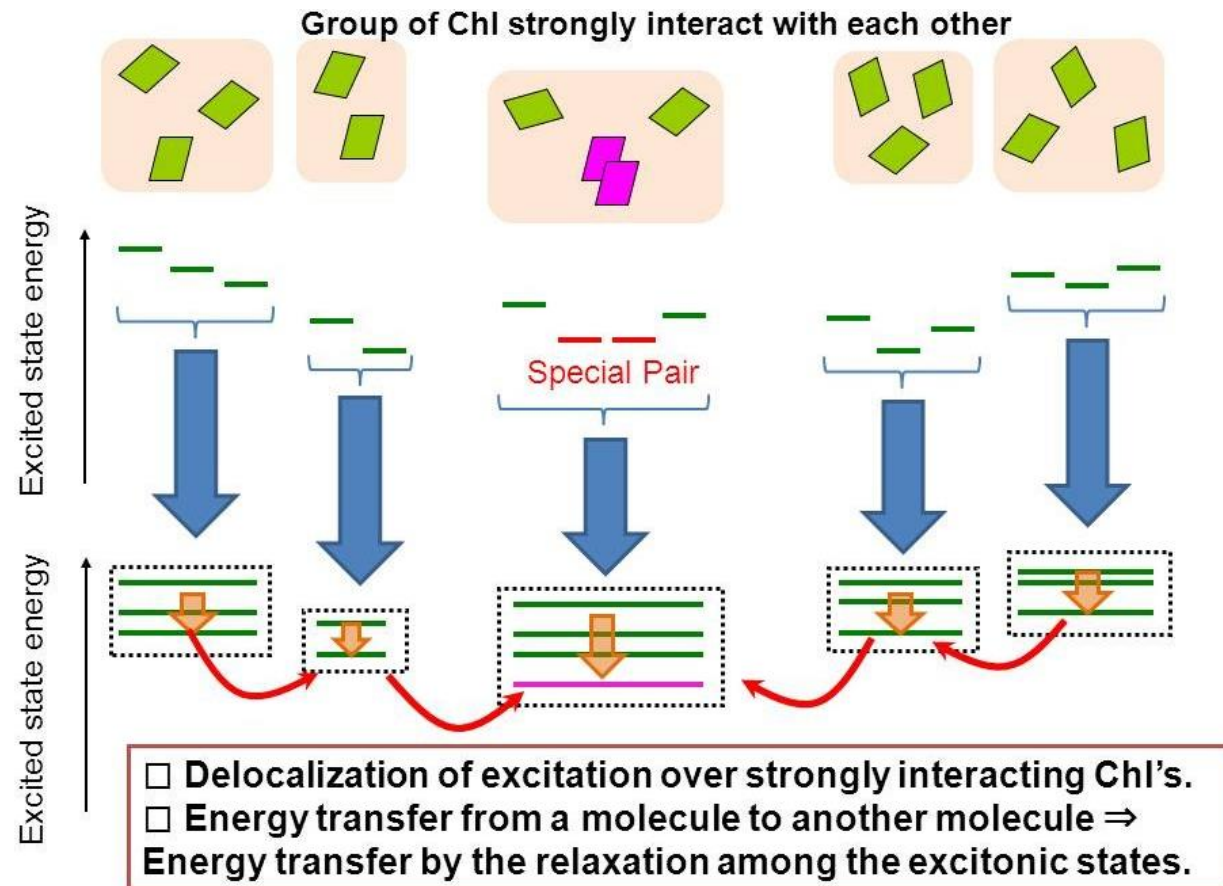


Su et al. 2017 Science

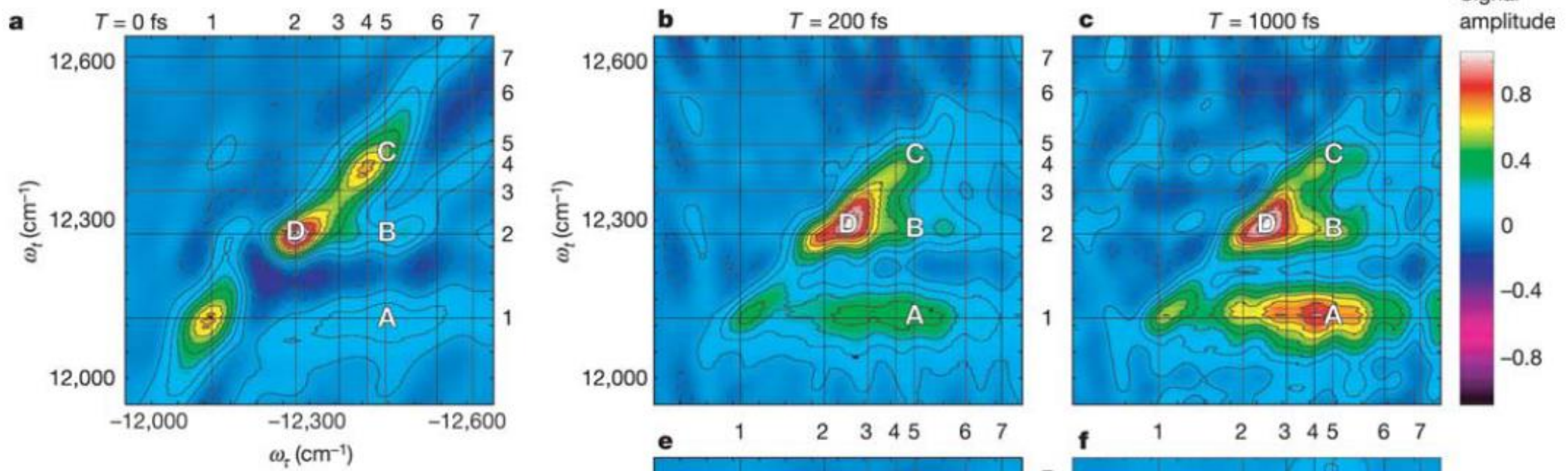
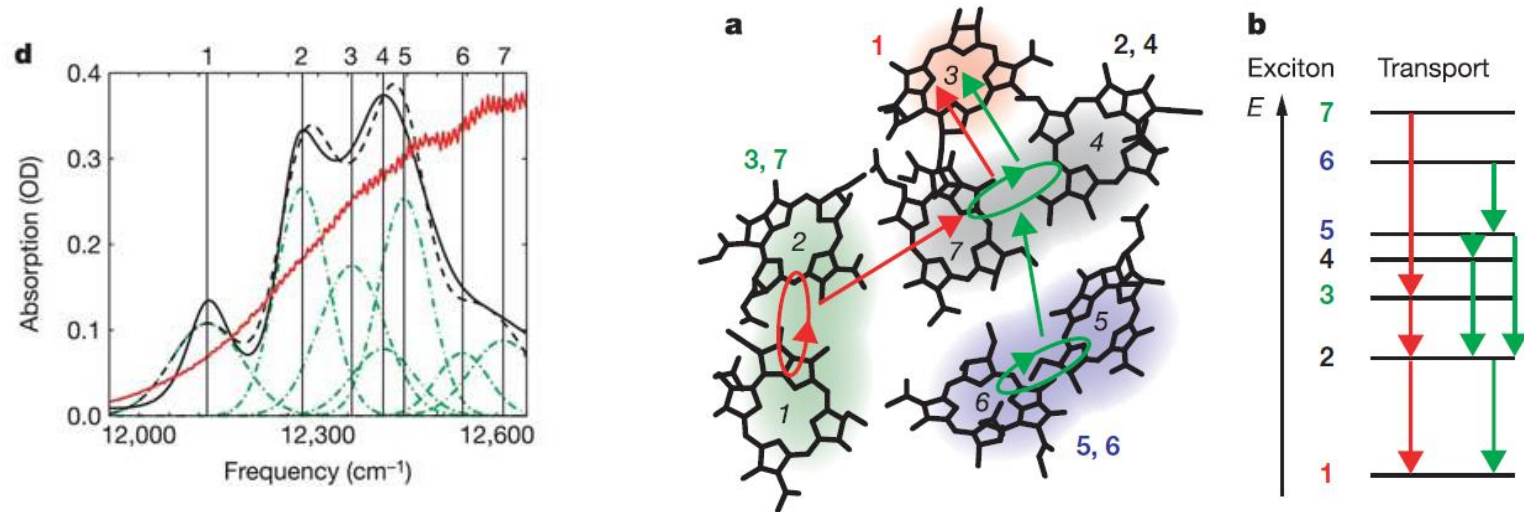
MOST OF THE CHLOROPHYLLS FUNCTION AS LIGHT-HARVESTING ANTENNA



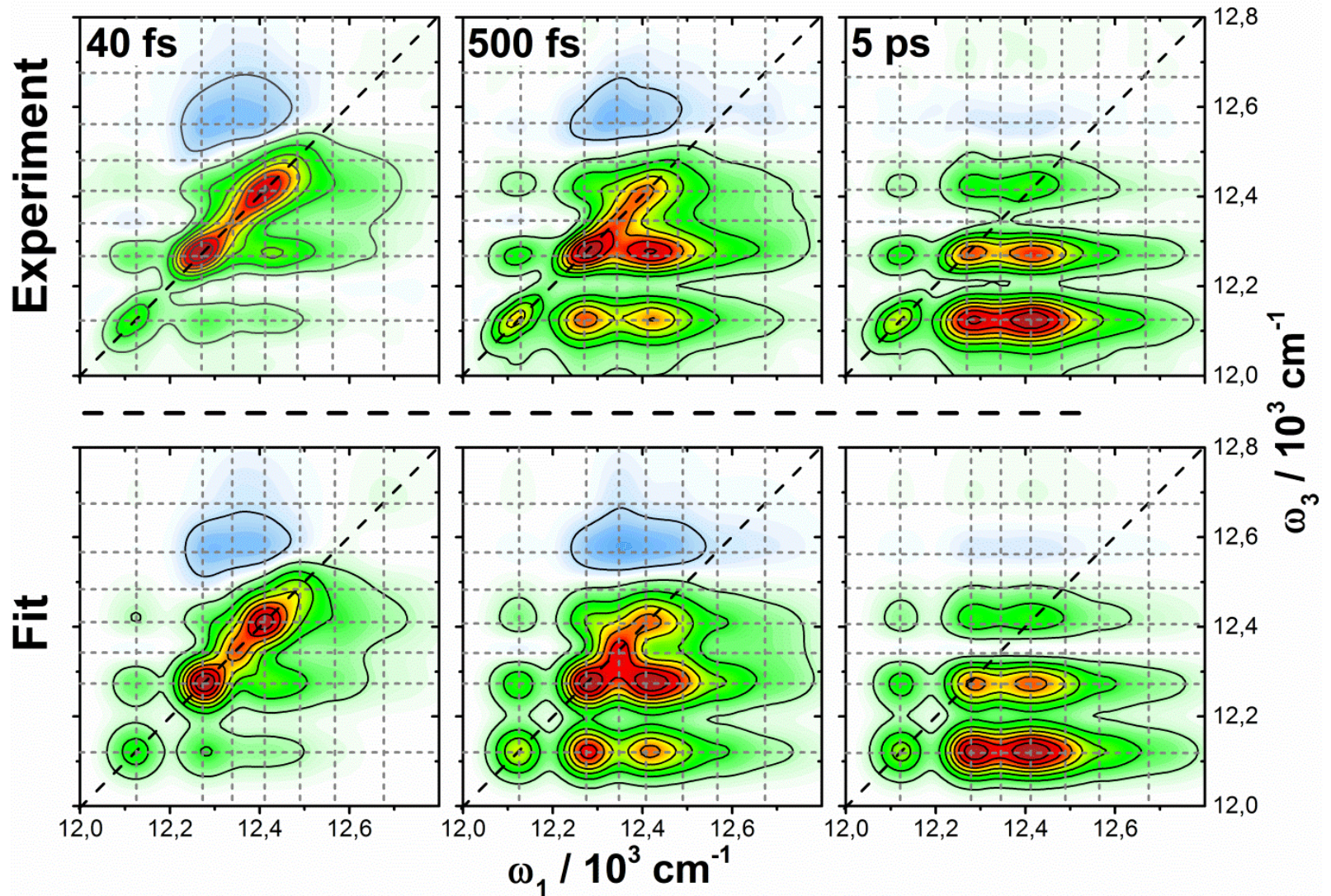
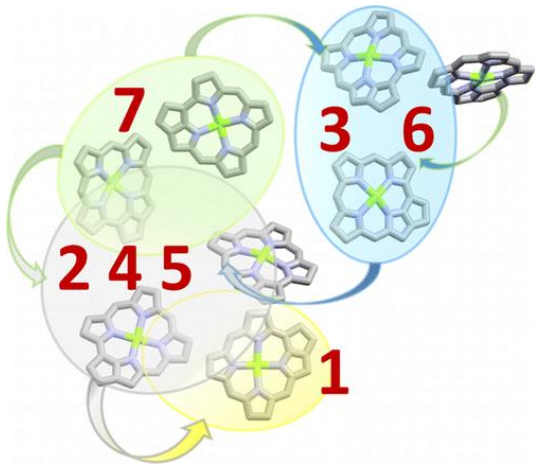
COHERENT AND INCOHERENT ENERGY TRANSFER



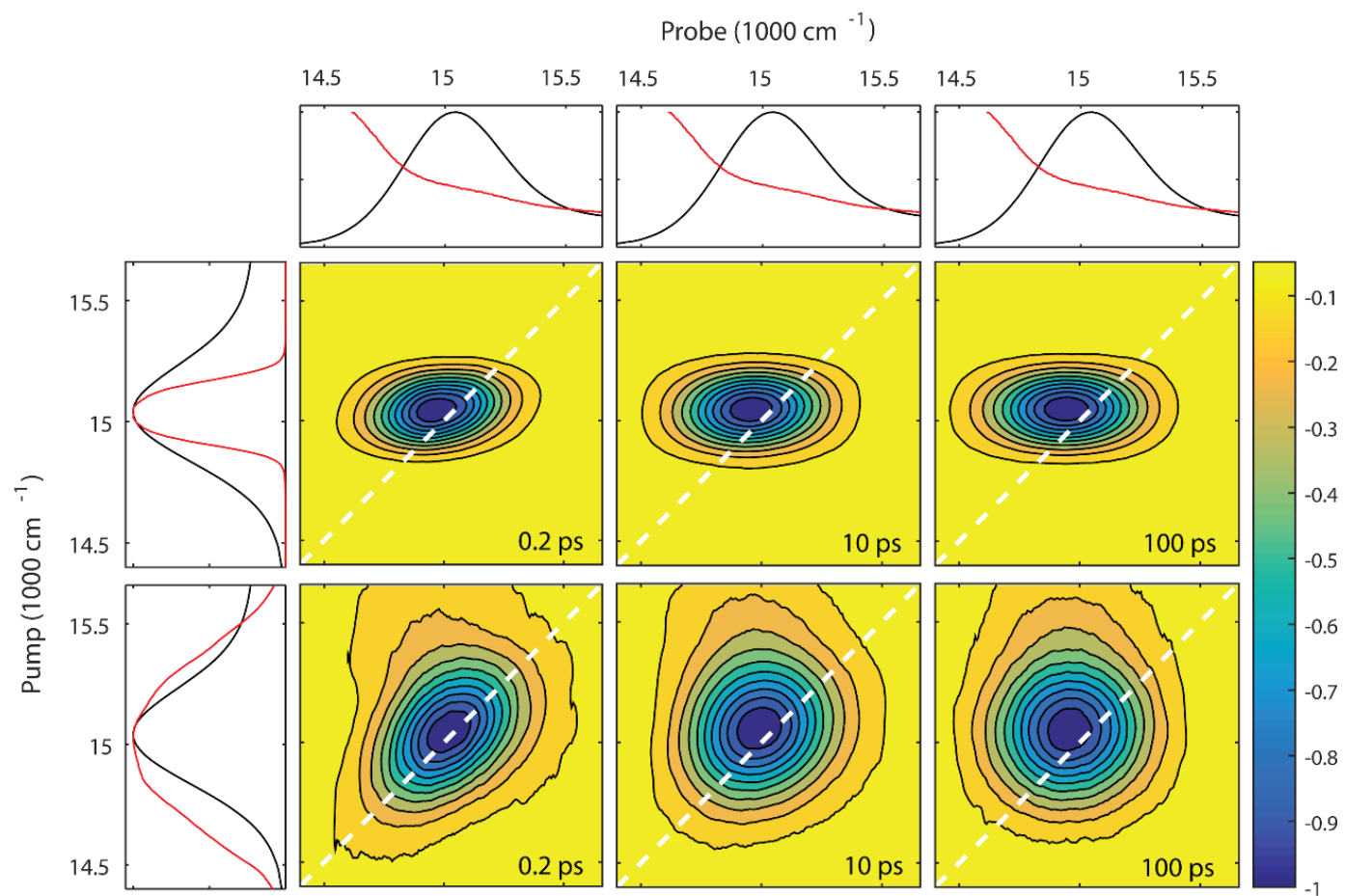
2D electronic spectroscopy of the FMO complex



ENERGY TRANSFER IN THE FENNA-MATHEWS-OLSON COMPLEX

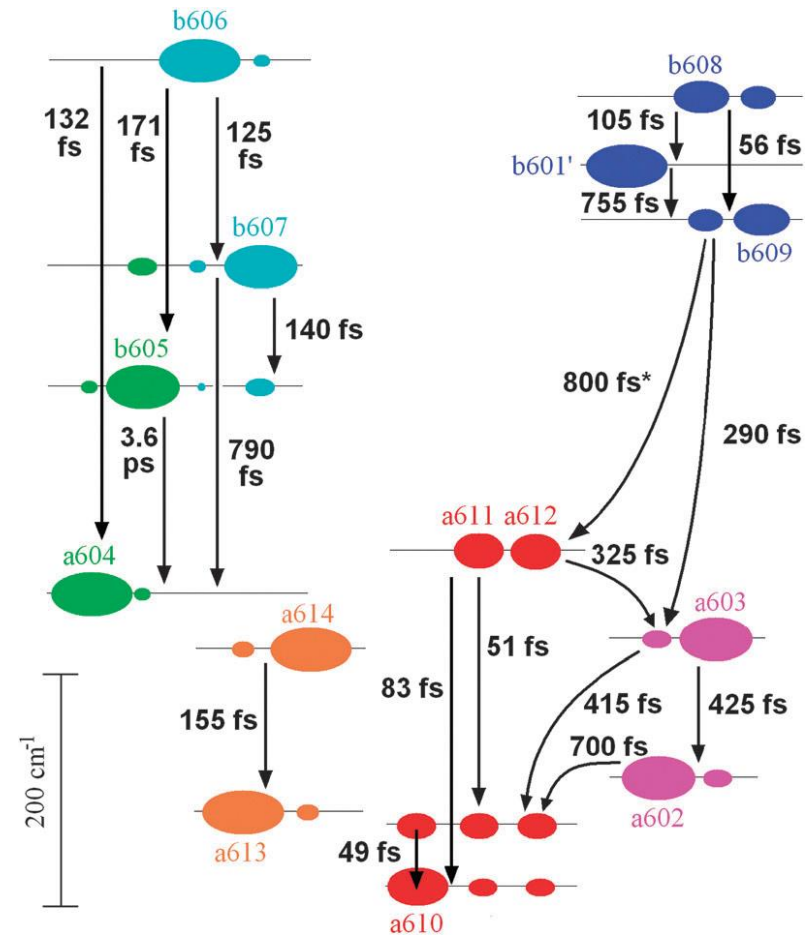
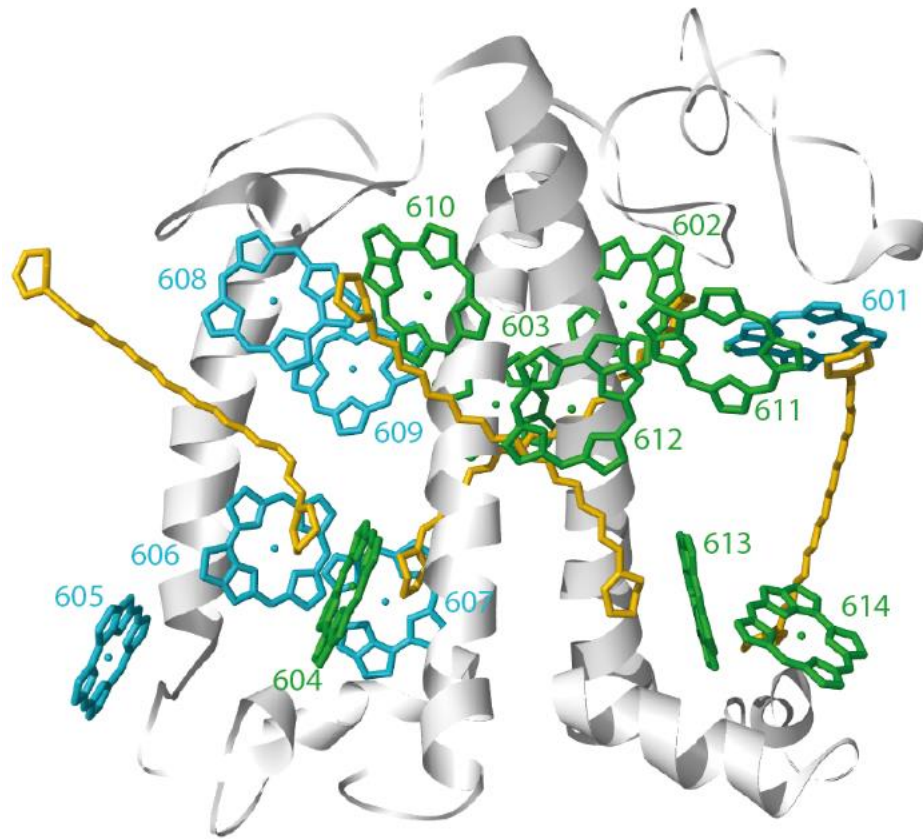


SPECTRAL DIFFUSION IN CHLOROPHYLL A



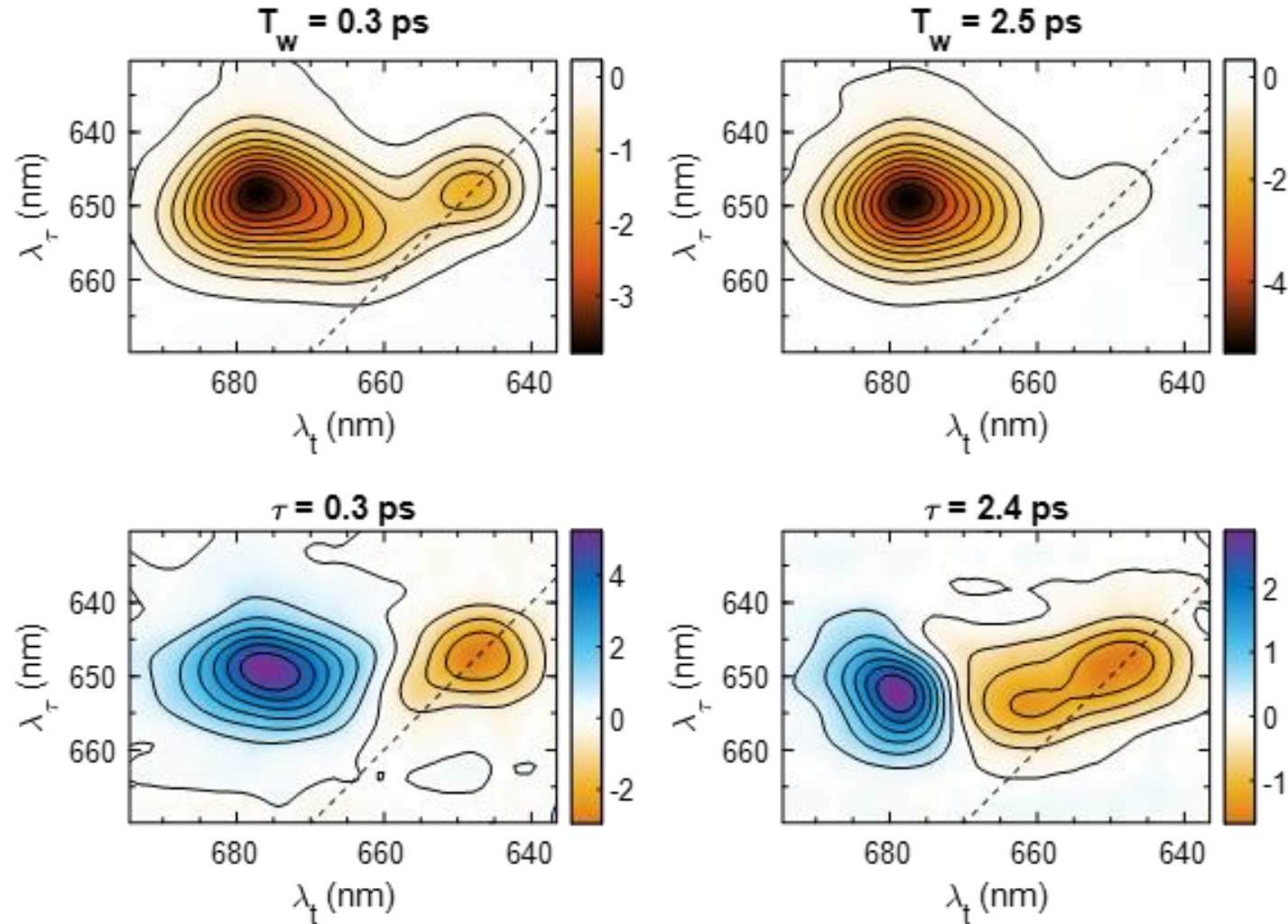
Nowakowski et al. (2018) *Chem Phys*

ENERGY TRANSFER IN LIGHT-HARVESTING COMPLEX II



Novoderezhkin et al. (2011) PCCP

2DES OF LHCII – CHLOROPHYLL B EXCITATION



Global lifetime analysis

$$S(\lambda_1, \lambda_3, t) = \sum_{i=1}^n A_i(\lambda_1, \lambda_3) e^{-\frac{t}{\tau}}$$

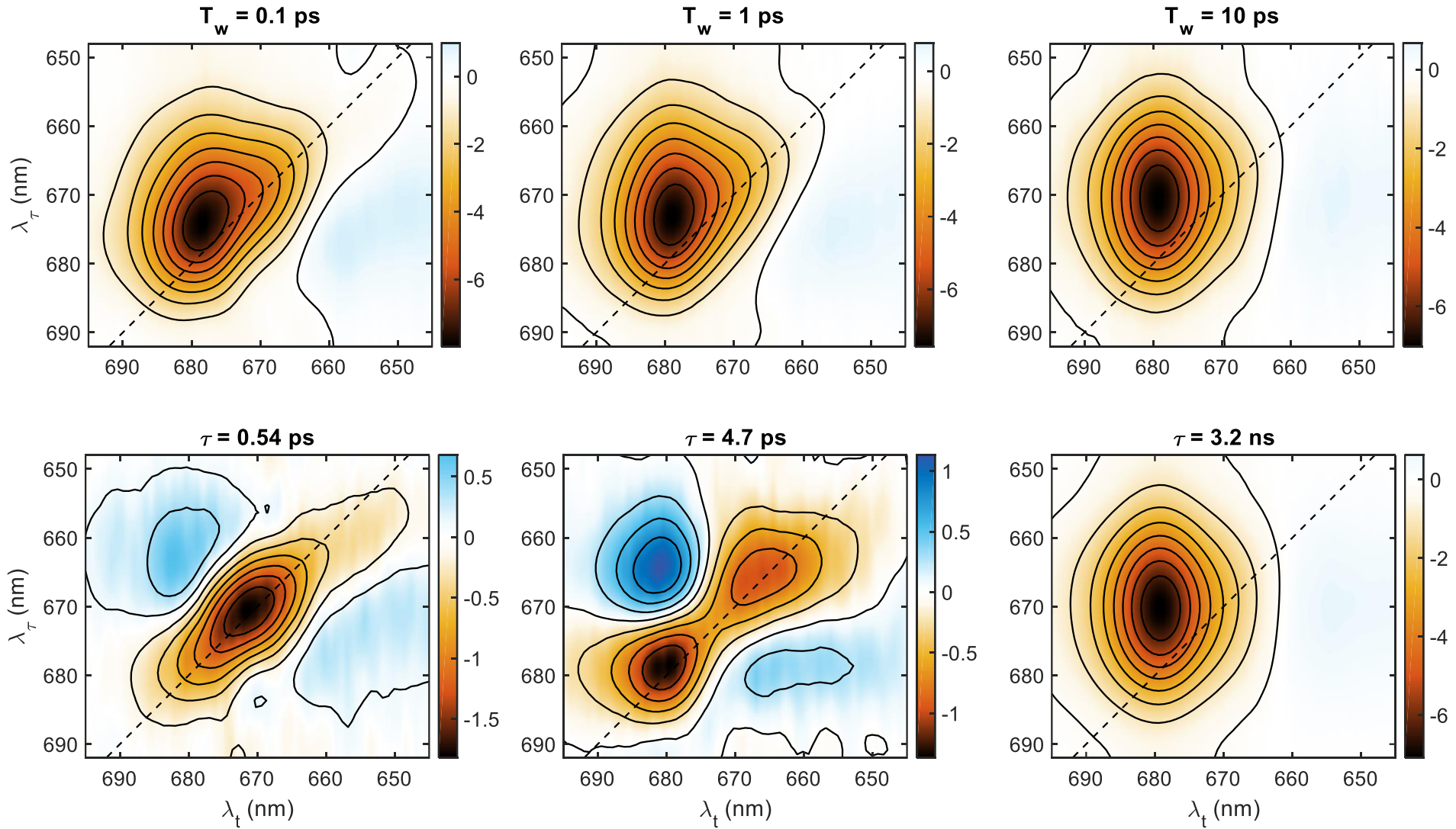
τ – lifetimes

$A_i(\lambda_1, \lambda_3)$ – 2D DAS

negative peaks – population decay

positive peaks – population rise

2D SPECTRA OF LHCII AT ROOM TEMPERATURE



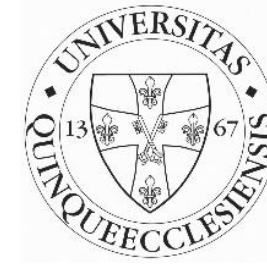
SUMMARY

2DES reveals information about:

- excitonic couplings between chromophores
- population dynamics (energy transfer) between chromophores
- coherent dynamics (exciton, vibrational and vibronic coherence)
- homogeneous and inhomogeneous broadening (energy disorder)
- dynamics of spectral diffusion
- bidirectional uphill/downhill energy transfer and thermal equilibration



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